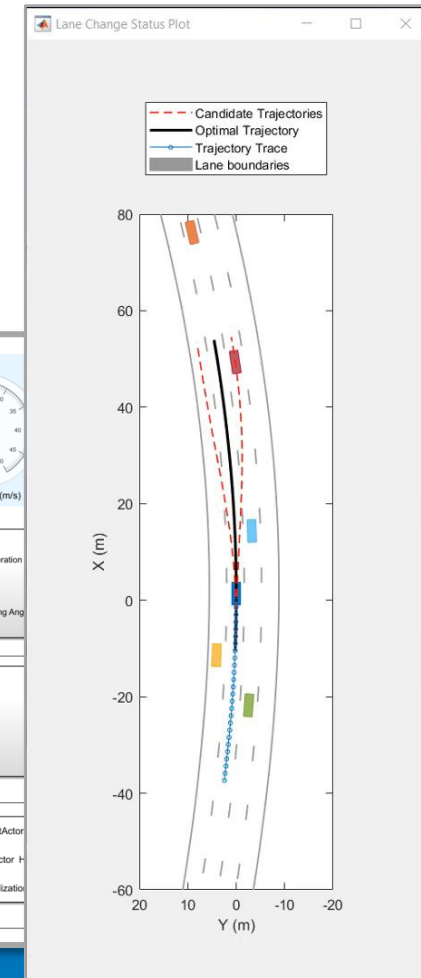
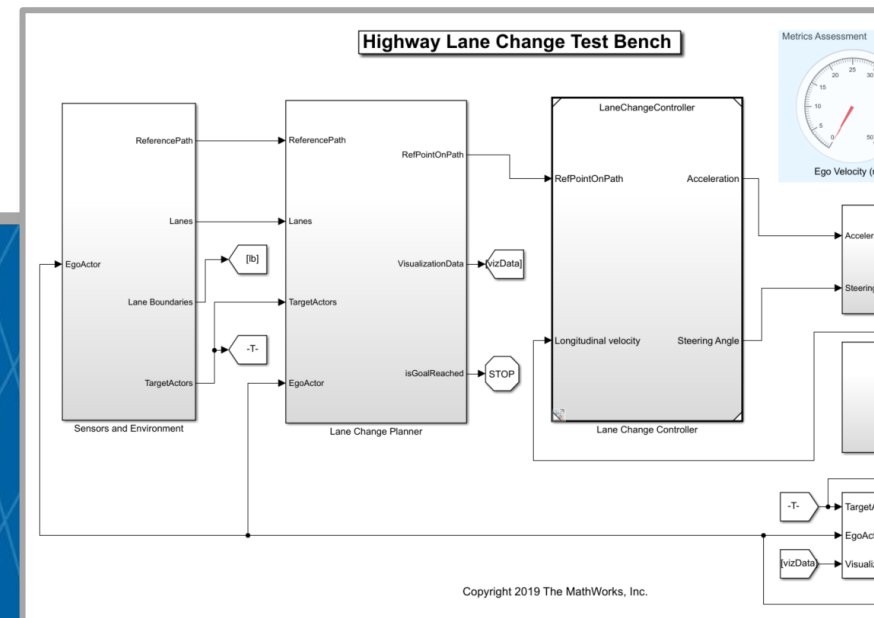
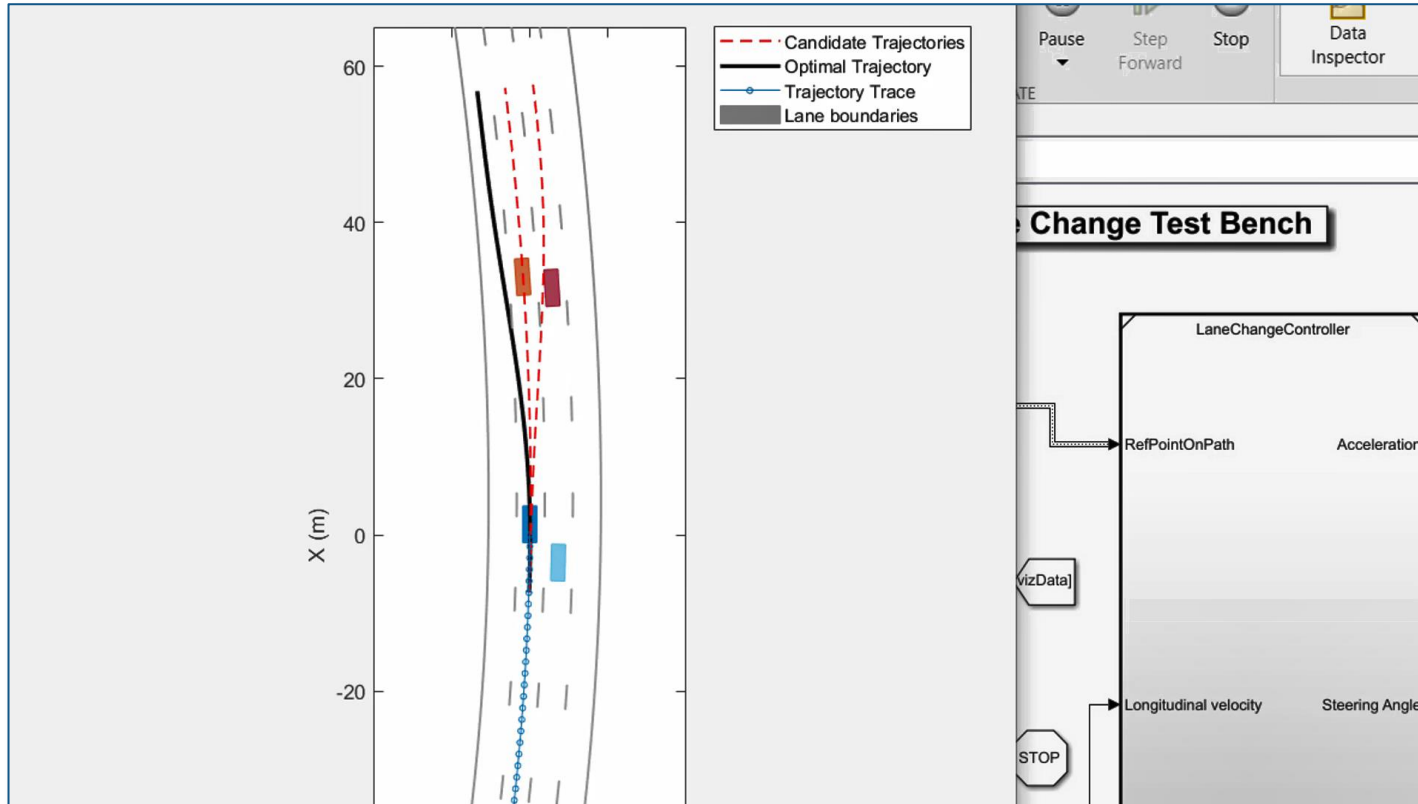


Developing Planning and Controls for Highway Lane Change Maneuvers

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 Application Engineering
 ADAS / Automated Driving
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Highway Lane Change



- Automated lane change maneuver (LCM) system for highway driving scenario (straight & curved roads)
- Generates a collision-free, optimal trajectory for lane change using trajectoryOptimalFrenet
- Behavior layer to configure motion planner
- State validator for collision checking
- Lane following controller using MPC

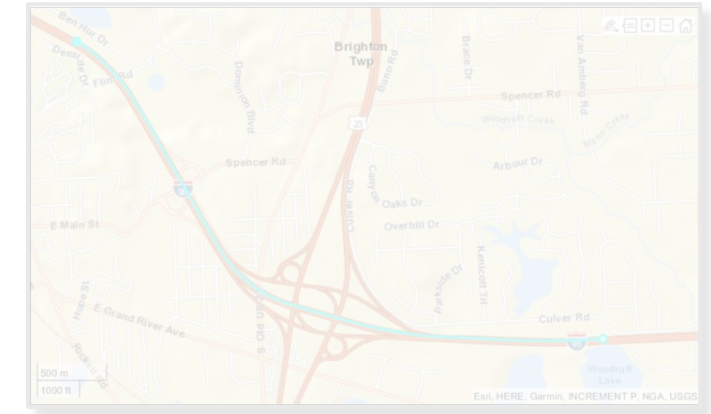
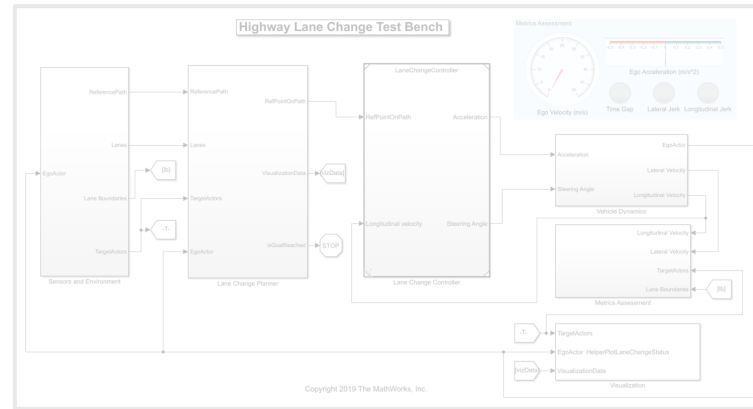
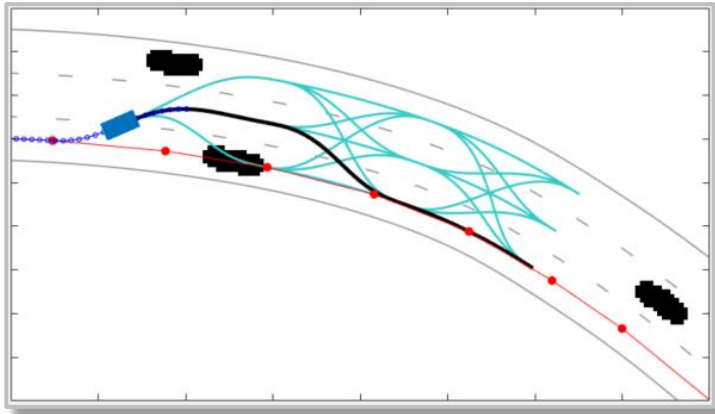
[Highway Lane Change](#)

Navigation Toolbox™

Model Predictive Control Toolbox™

Automated Driving Toolbox™

Highway Lane Change



Learn motion planner

- Optimal trajectory generation in Frenet coordinate
- Planner parameters
- Simulate trajectory planning with occupancy map

Integrate motion planner and controller

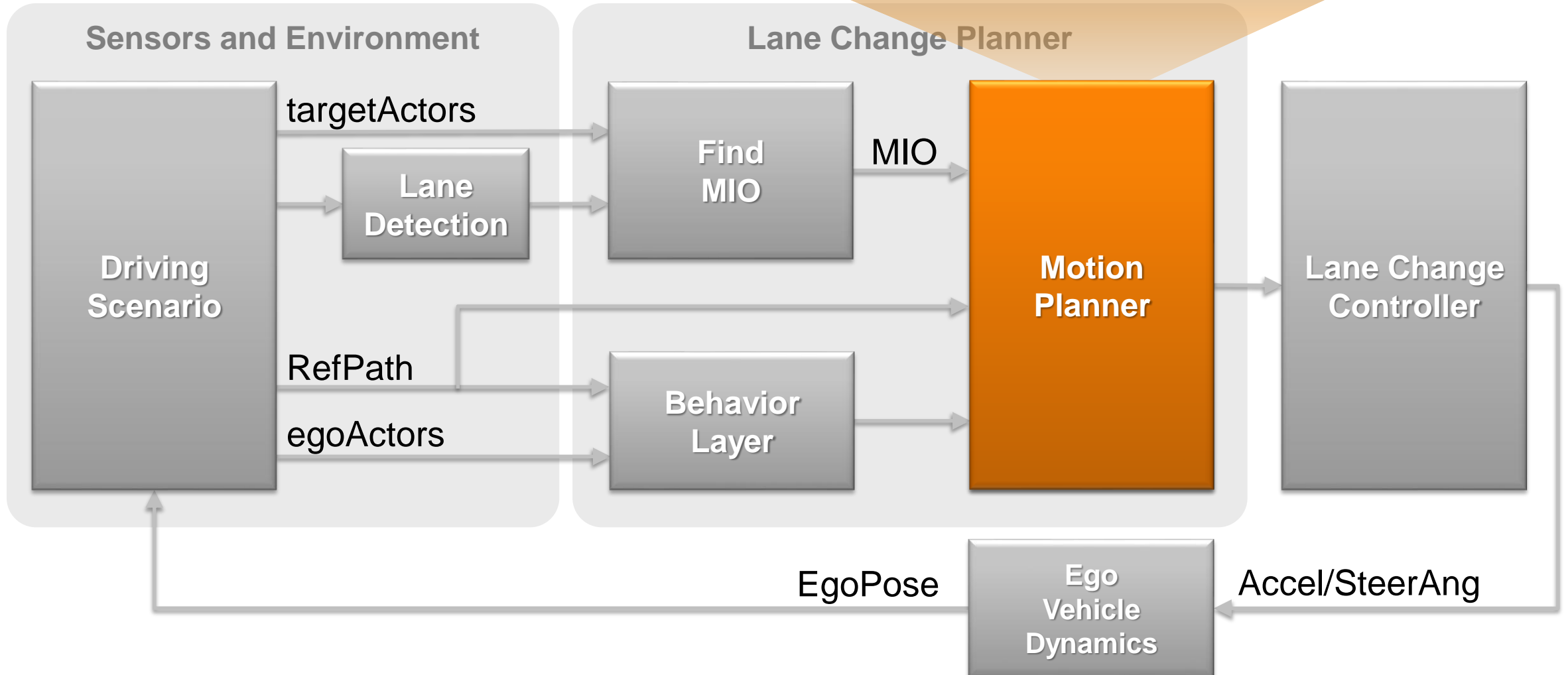
- Learn through reference example
- Architecture of highway lane change
- Simulate closed-loop controller with test scenarios

Test with real-world scenario

- Create scenario from HD map
- Update setup script and model
- Run simulation with new scenario

Architecture of Highway Lane Change

```
planner = trajectoryOptimalFrenet(refPath, validator)
```



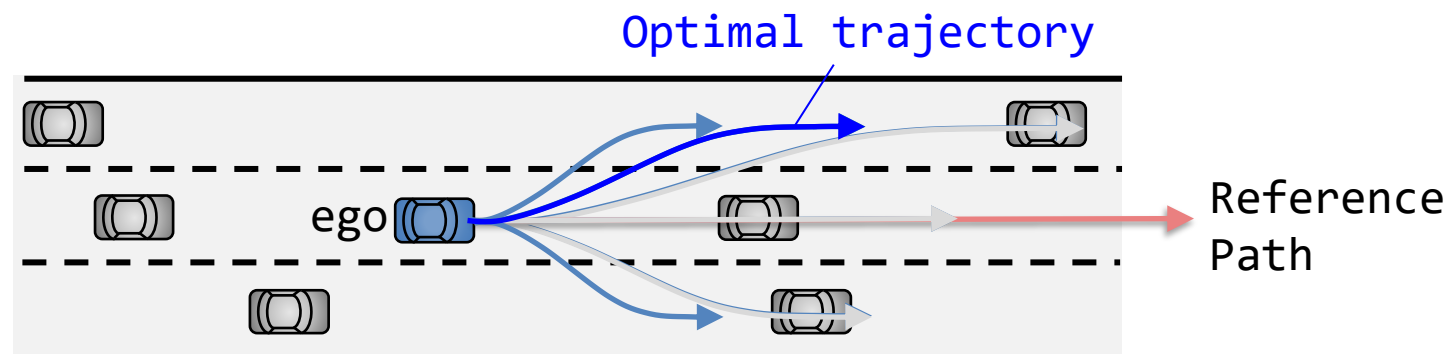
Optimal Trajectory Generation

- trajectoryOptimalFrenet function generates an **optimal, feasible, and collision-free** trajectory for the reference path

```
planner = trajectoryOptimalFrenet(refPath, validator)
```

reference path

state validator
for collision checking



State Validator for collision checking

```
% Create a state validator object for collision checking
stateValidator = validatorOccupancyMap;
```

```
% Create and Assign binaryOccupancyMap to the state validator
stateValidator.Map = binaryOccupancyMap(width,height);
```

1) Assign 2-D occupancy grid map with binary values

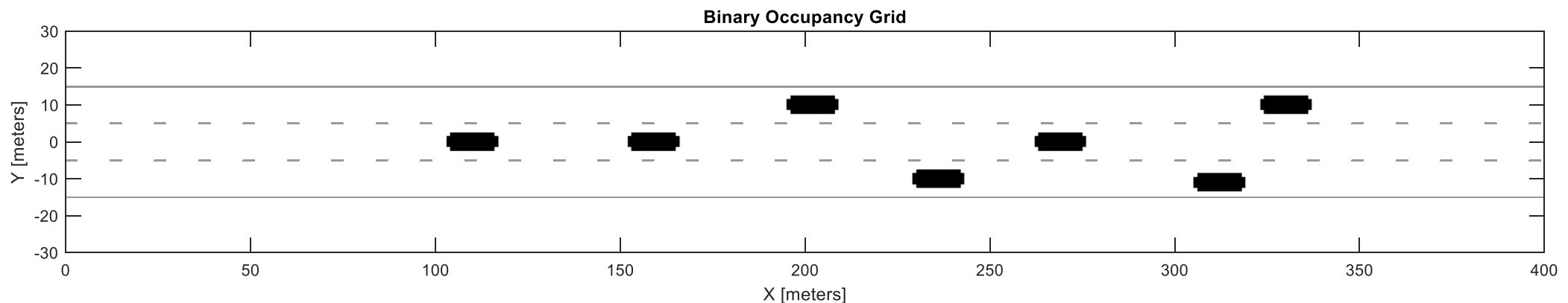
```
% Or, use occupancyMap
stateValidator.Map = occupancyMap(width,height);
```

2) Assign 2-D occupancy grid map with probabilistic values (0..1)

```
% Or, create a custom state validator object
stateValidator = MyCustomStateValidator;
```

3) Use custom state validator

```
classdef MyCustomStateValidator < nav.StateValidator & ...
    matlabshared planning_internal_EnforceScalarHandle
```



Planner parameters

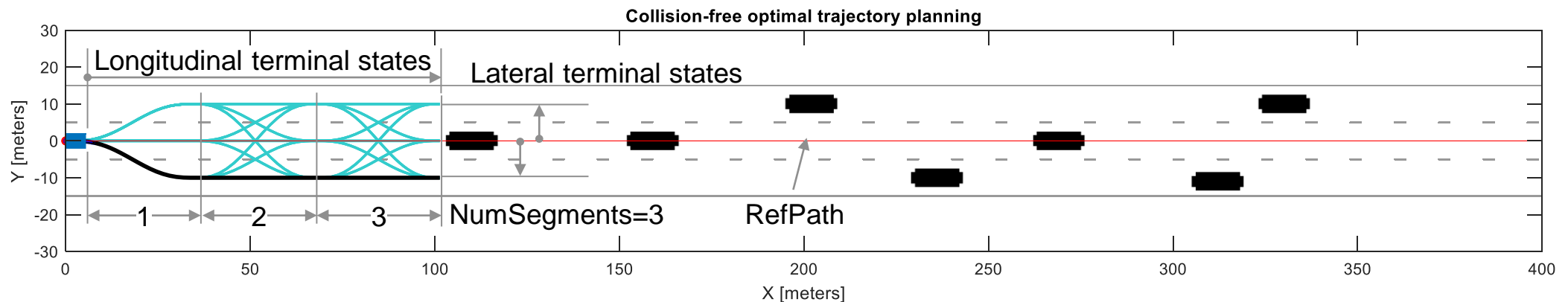
- Terminal states
- No. of longitudinal segments
- Feasibility parameters

```

% Assign terminal states for longitudinal state, lateral deviation,
% speed, time, and acceleration
planner.TerminalStates.Longitudinal = 100;
planner.TerminalStates.Lateral = -10:10:10;
planner.TerminalStates.Speed = 8;
planner.TerminalStates.Time = 7;
planner.TerminalStates.Acceleration = 0;

% Assign number of partitions for the longitudinal terminal state
planner.NumSegments = 3;

% Assign maximum acceleration and curvature values for feasibility
planner.FeasibilityParameters.MaxCurvature = 0.1;
planner.FeasibilityParameters.MaxAcceleration = 10;
    
```



Optimal Trajectory Generation

```
trajectory = plan(planner, startFrenetState)
```

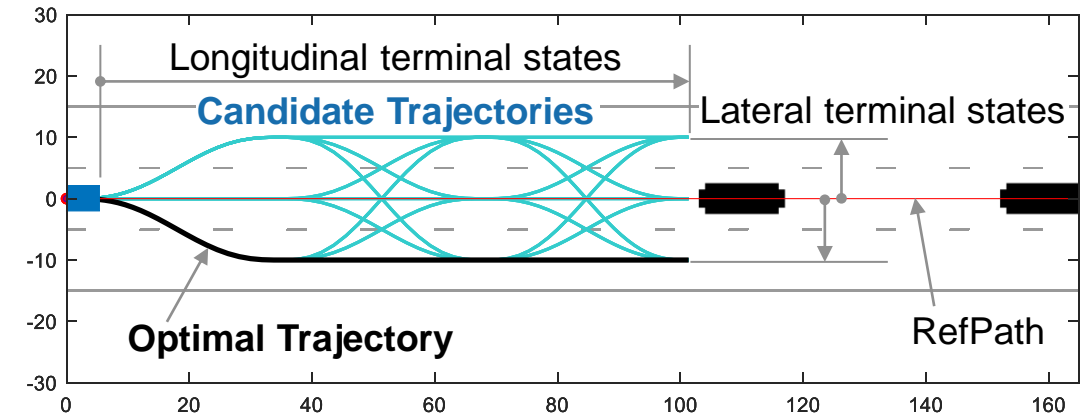
Samples multiple candidate trajectories for each pair of states (start, terminal states)

Evaluate **cost** for all candidate trajectories

Check **feasibility** for all candidate trajectories

Check **collision** using **state validator**

Choose a **feasible trajectory with the least cost**
→ optimal, feasible, and collision-free trajectory



Cost weights

- Time, Arc length, Deviation
- Lateral/longitudinal smoothness

Feasibility parameters:

- MaxCurvature, MaxAcceleration

validatorOccupancyMap

Custom state validator

Generate trajectory in Frenet coordinate using quintic polynomial

- Quintic polynomial

$$s(t) = a_5 t^5 + a_4 t^4 + a_3 t^3 + a_2 t^2 + a_1 t + a_0$$

$$\dot{s}(t) = 5a_5 t^4 + 4a_4 t^3 + 3a_3 t^2 + 2a_2 t + a_1$$

$$\ddot{s}(t) = 20a_5 t^3 + 12a_4 t^2 + 6a_3 t + 2a_2$$

where s = longitudinal or lateral distance

- Start boundary conditions ($t = 0$)

$$a_0 = s_{start}$$

$$a_1 = \dot{s}_{start}$$

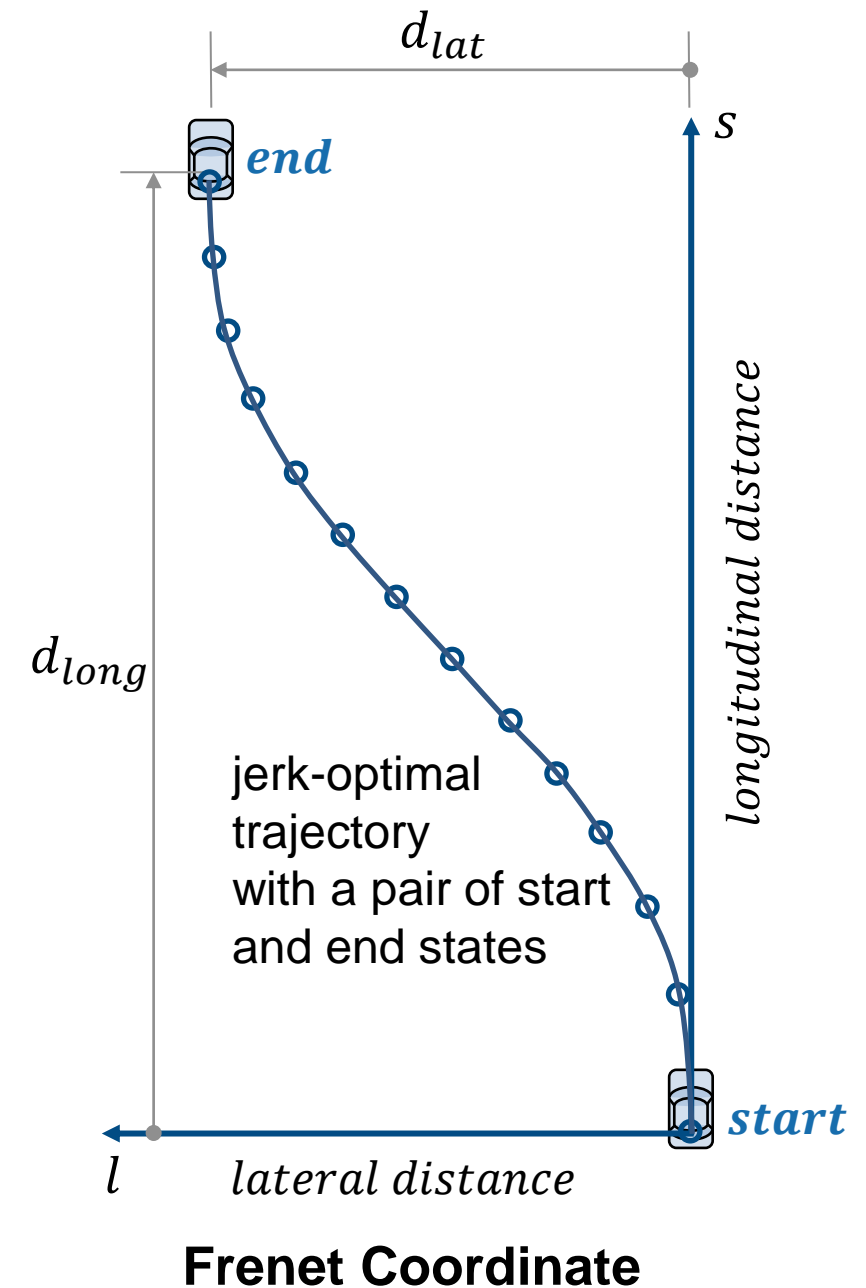
$$2a_2 = \ddot{s}_{start}$$

- End boundary conditions ($t = t_f$)

$$a_5 t_f^5 + a_4 t_f^4 + a_3 t_f^3 + a_2 t_f^2 + a_1 t_f + a_0 = s_{end}$$

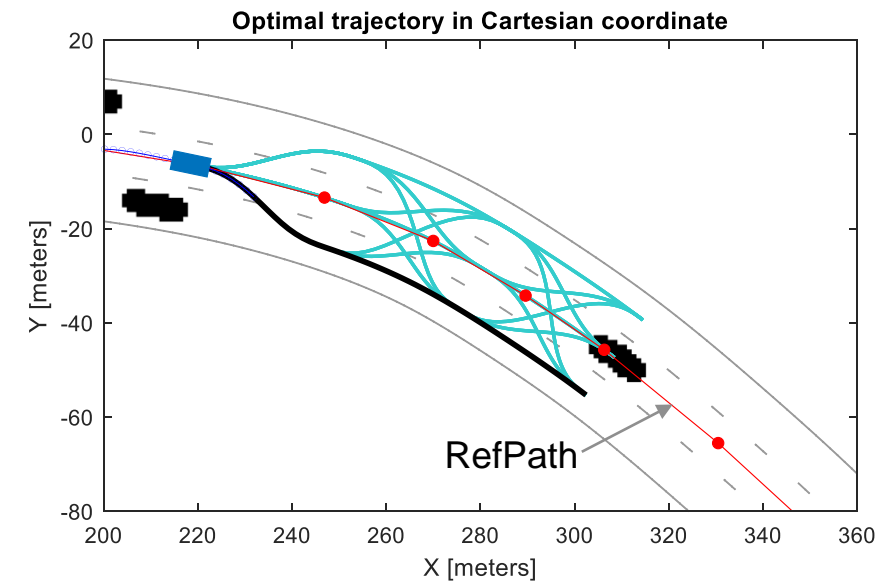
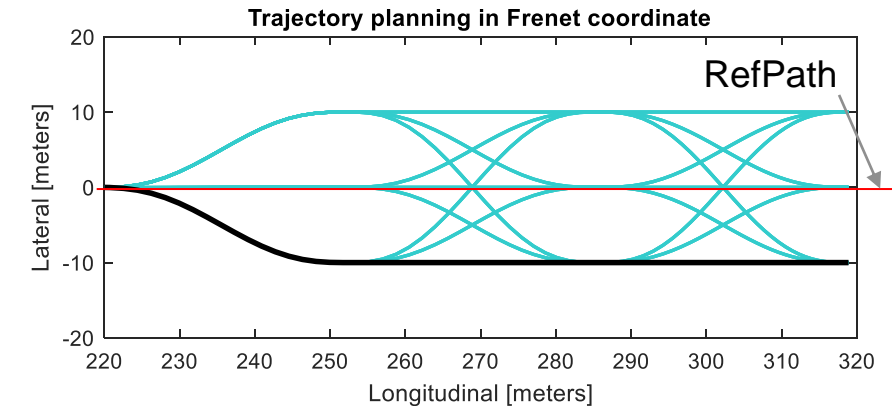
$$5a_5 t_f^4 + 4a_4 t_f^3 + 3a_3 t_f^2 + 2a_2 t_f + a_1 = \dot{s}_{end}$$

$$20a_5 t_f^3 + 12a_4 t_f^2 + 6a_3 t_f + 2a_2 = \ddot{s}_{end}$$

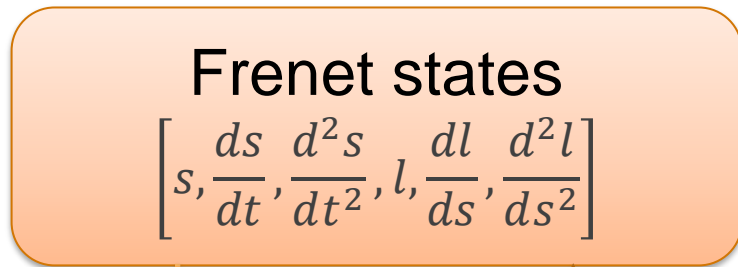


Advantage of trajectory generation in Frenet coordinate

- Frenet system represents an object and its trajectory with respect to the reference path (road center or lane center).
- This approach dramatically simplifies the problem of trajectory generation when a car is traveling on a curved road.



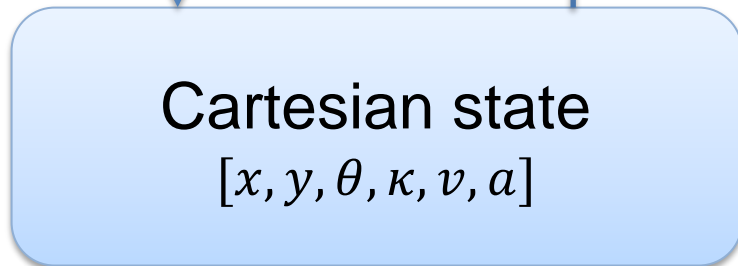
Convert Frenet states \leftrightarrow Cartesian states



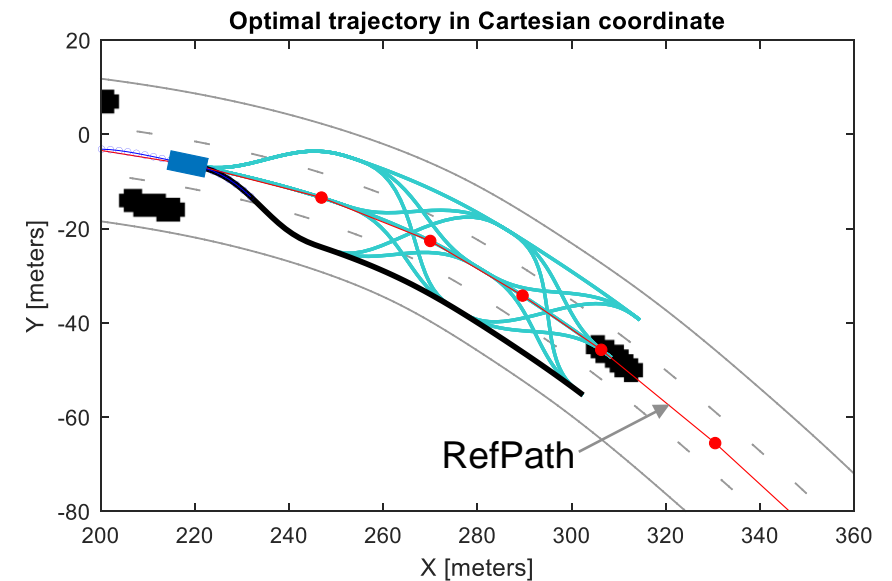
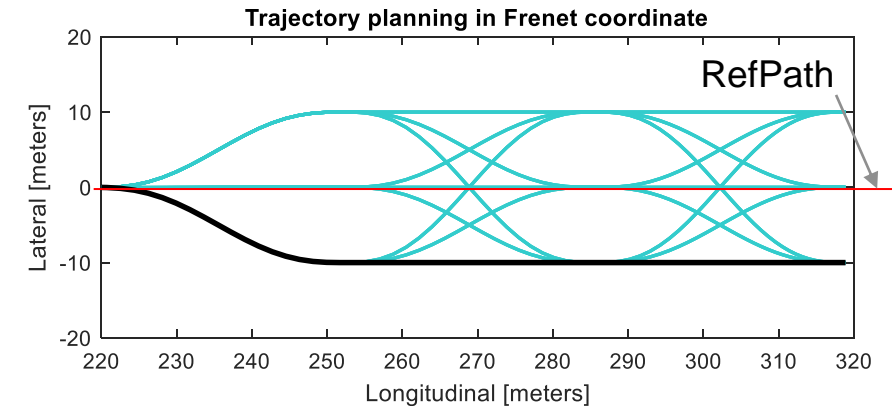
- s : arc length (longitudinal distance)
- l : normal distance (lateral distance) from reference path

frenet2cart

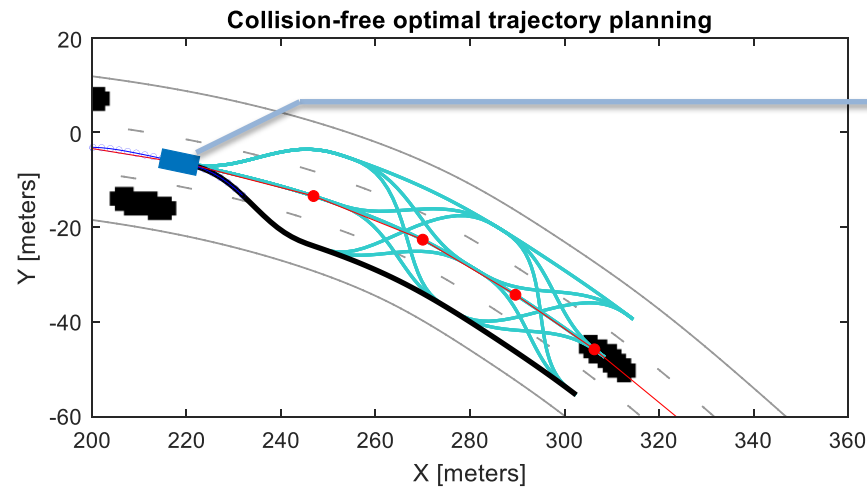
cart2frenet



- x, y : position in meters
- θ : orientation angle in radians
- κ : curvature in m^{-1}
- v : velocity in m/s
- a : acceleration in m/s^2



Convert Frenet states \leftrightarrow Cartesian states



Current Cartesian state
 $[x, y, \theta, \kappa, v, a]$

cart2frenet

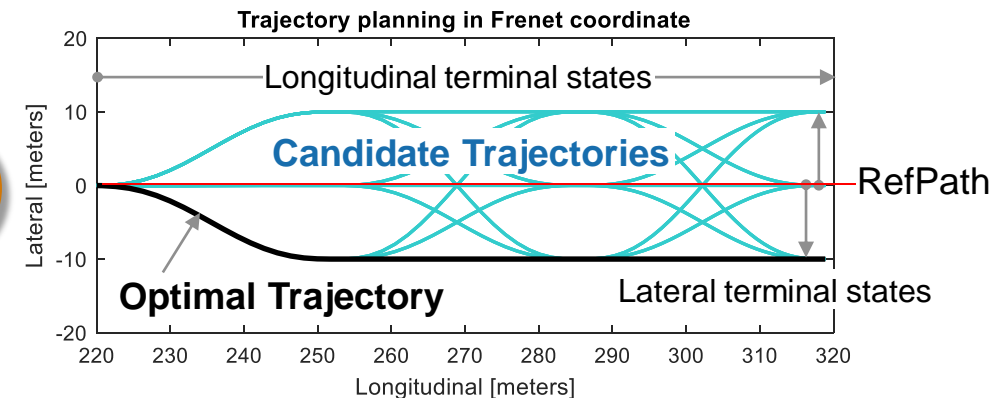
Start Frenet state
 $\left[s, \frac{ds}{dt}, \frac{d^2s}{dt^2}, l, \frac{dl}{ds}, \frac{d^2l}{ds^2} \right]$

Optimal trajectory
 in Cartesian state
 $[x, y, \theta, \kappa, v, a, t]$

`trajectory = plan(planner, startFrenetState)`

frenet2cart

Trajectory generation
 in Frenet states



Optimal Trajectory Planning in Frenet Space

- shipping example

```
% Step 1) Create and Assign Map to State Validator
```

```
% Step 2) Initialize the planner object and set planner parameters
```

```
% Step 3) Trajectory Planning
```

```
% Step 4) Trajectory Visualization
```

```
% Visualize the map and the trajectories.
```

```
show(map)
```

```
hold on
```

```
show(planner, 'Trajectory', 'all')
```

```
% and the custom cost function.
```

```
planner =
```

```
trajectoryOptimalFrenet(refPath, stateValida
```

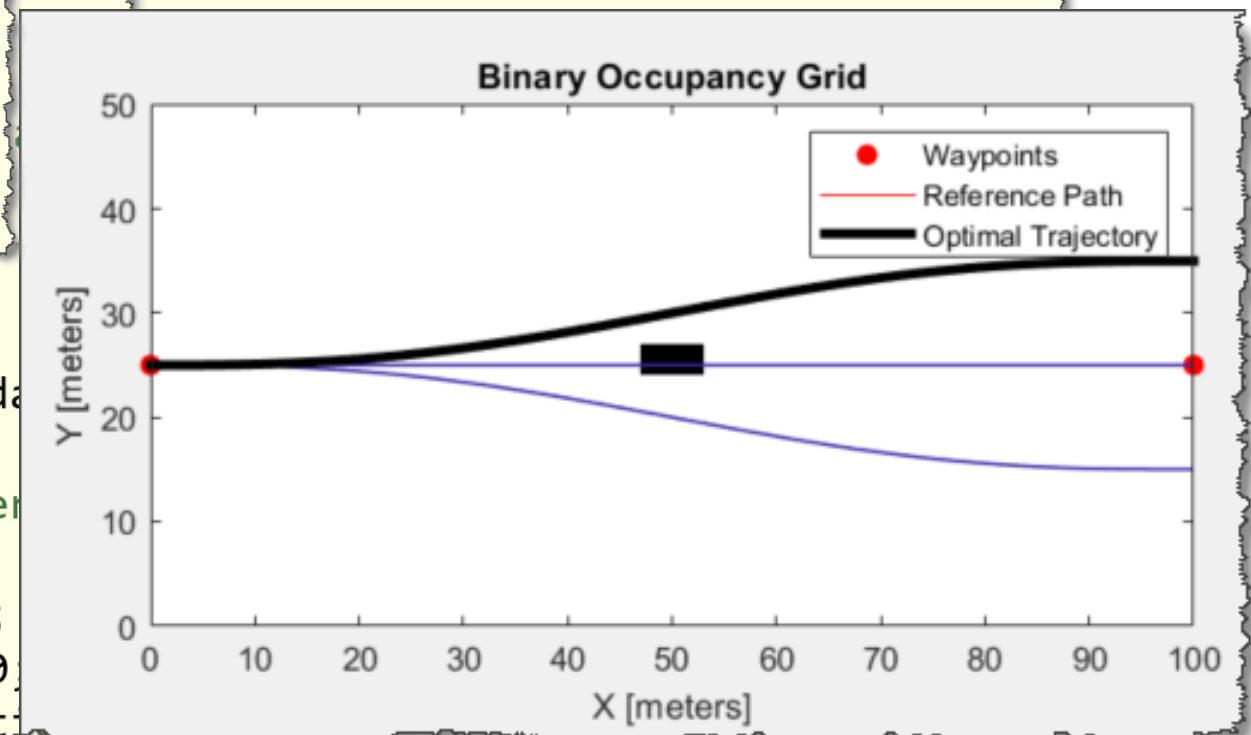
```
% Assign longitudinal terminal state, later  
% values.
```

```
planner.TerminalStates.Longitudinal = 100;
```

```
planner.TerminalStates.Lateral = -10:10:10
```

```
planner.FeasibilityParameters.MaxAccelerat
```

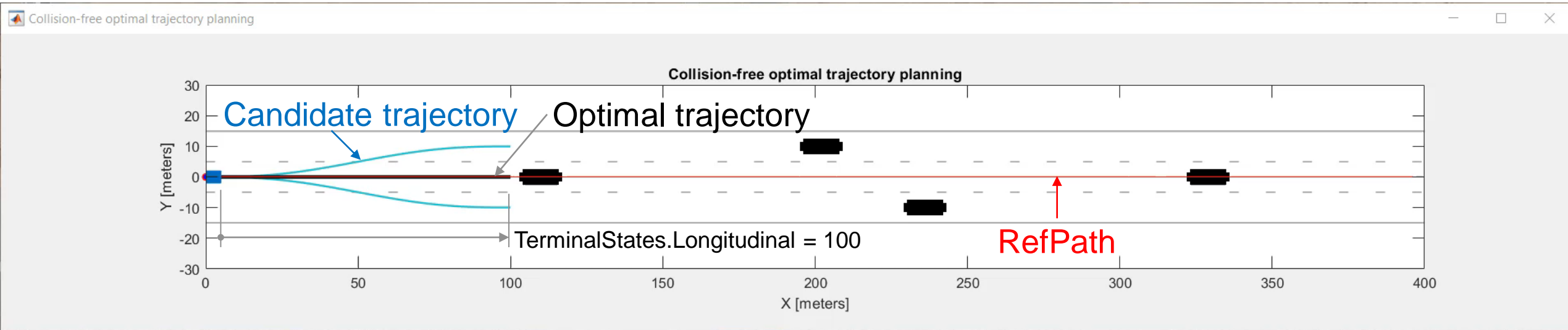
llow.



Optimal Trajectory Planning with binary occupancy map

: Straight road

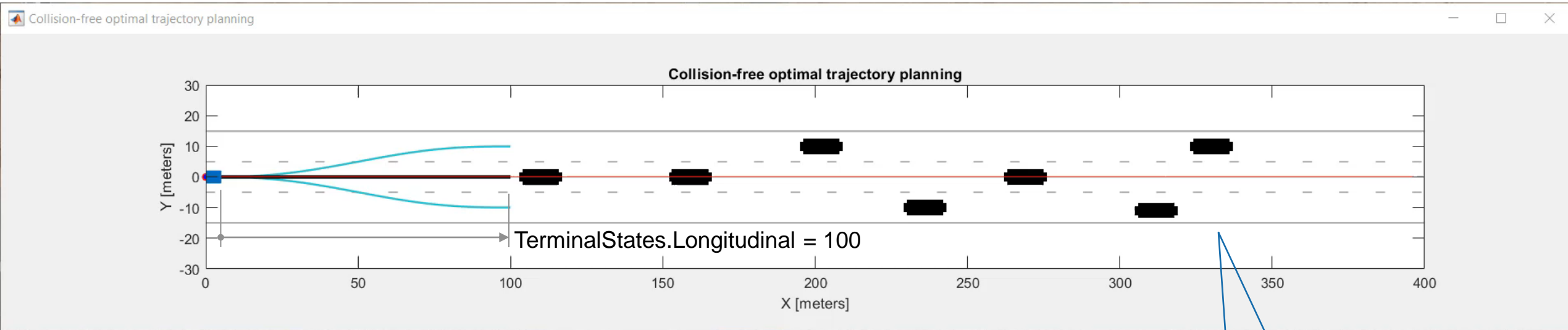
- TerminalStates.Longitudinal = 100
- NumSegments = 1



Optimal Trajectory Planning with binary occupancy map

: Straight road with dense traffic condition

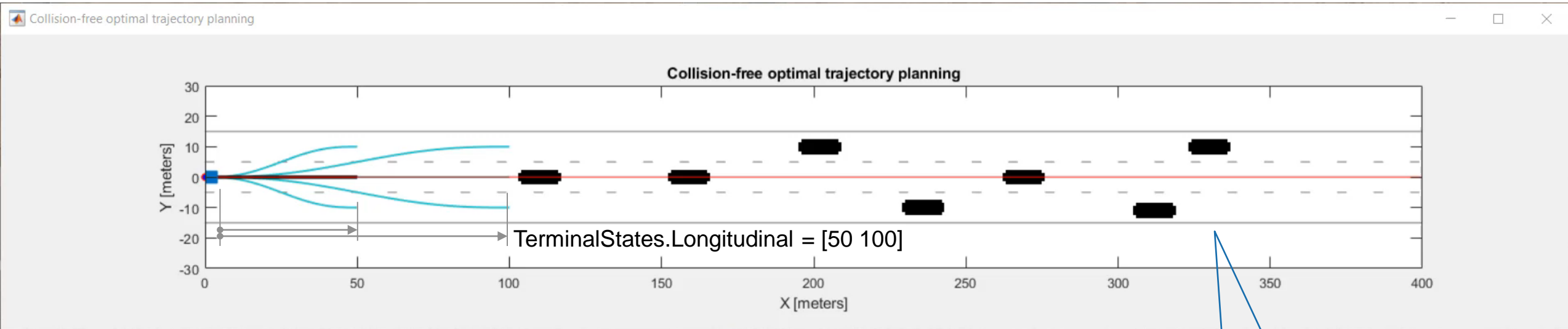
- TerminalStates.Longitudinal = 100
- NumSegments = 1



Optimal Trajectory Planning with binary occupancy map

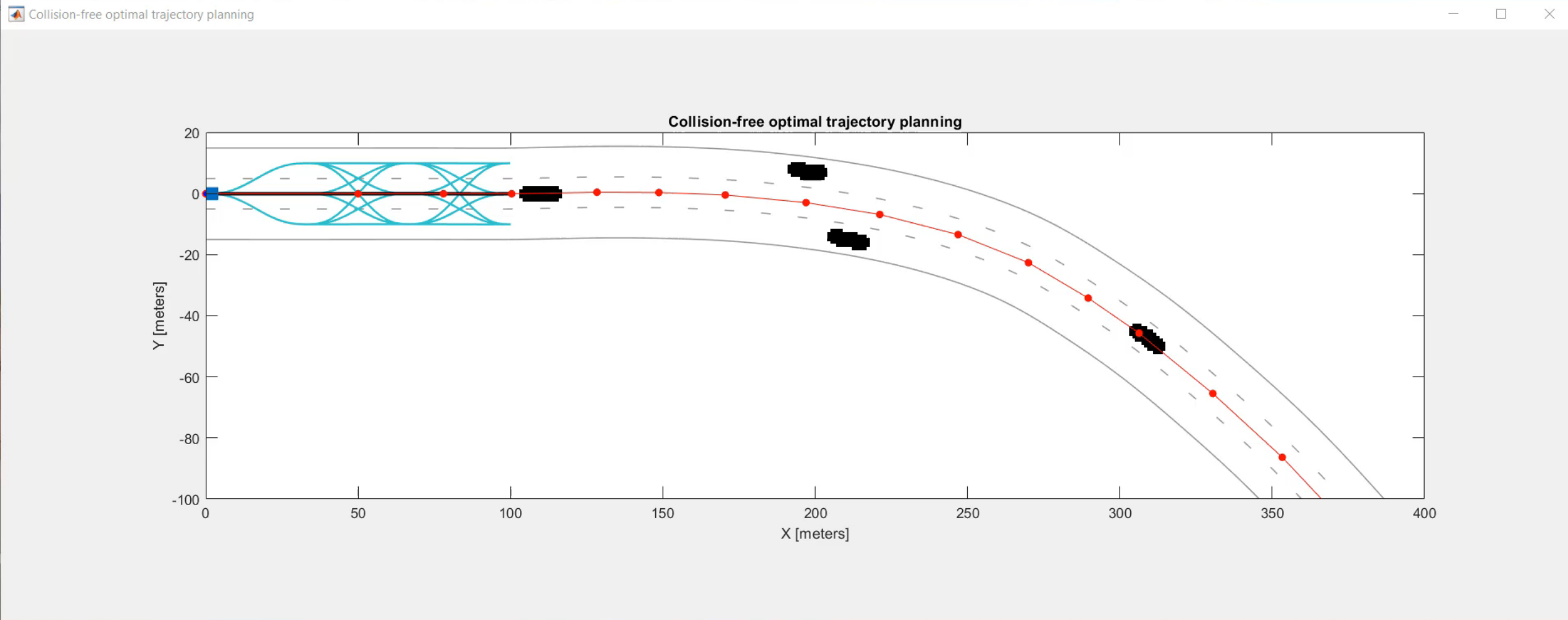
: Straight road with dense traffic condition

- TerminalStates.Longitudinal = [50 100]
- NumSegments = 1

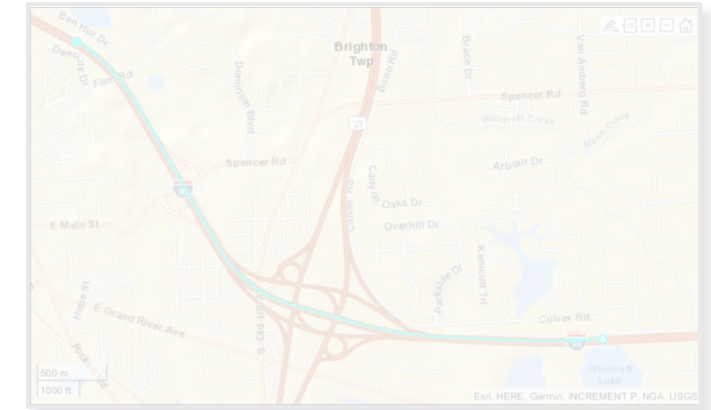
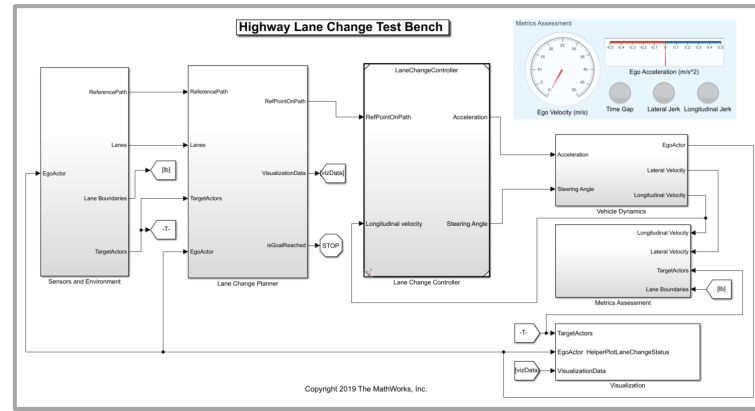
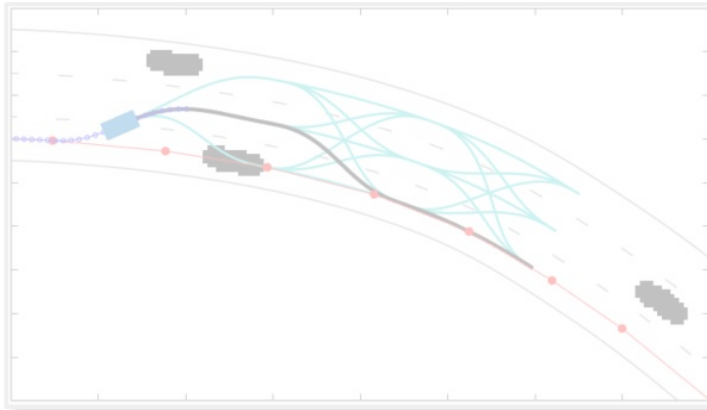


Optimal Trajectory Planning with binary occupancy map : Curved road

- TerminalStates.Longitudinal = 100
- NumSegments = 3



Highway Lane Change



Learn motion planner

- Optimal trajectory generation in Frenet coordinate
- Planner parameters
- Simulate trajectory planning with occupancy map

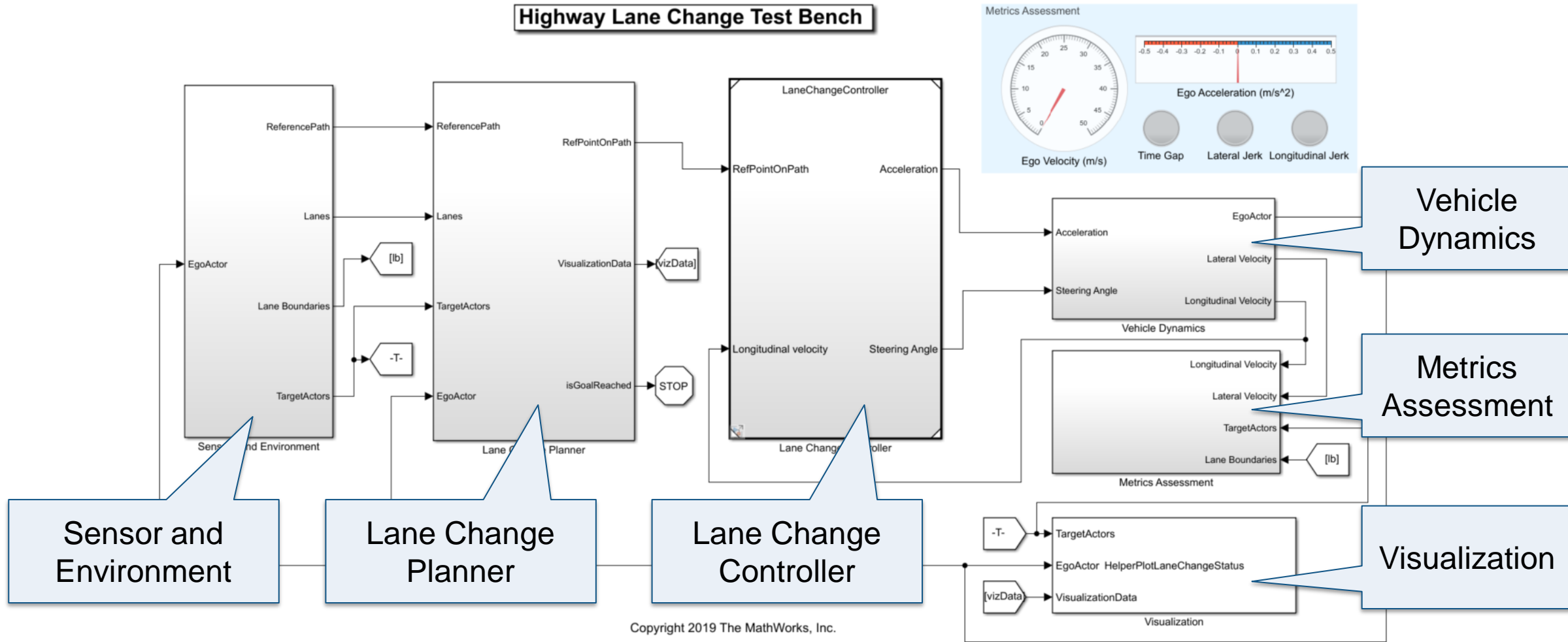
Integrate motion planner and controller

- Learn through reference example
- Architecture of highway lane change
- Simulate closed-loop controller with test scenarios

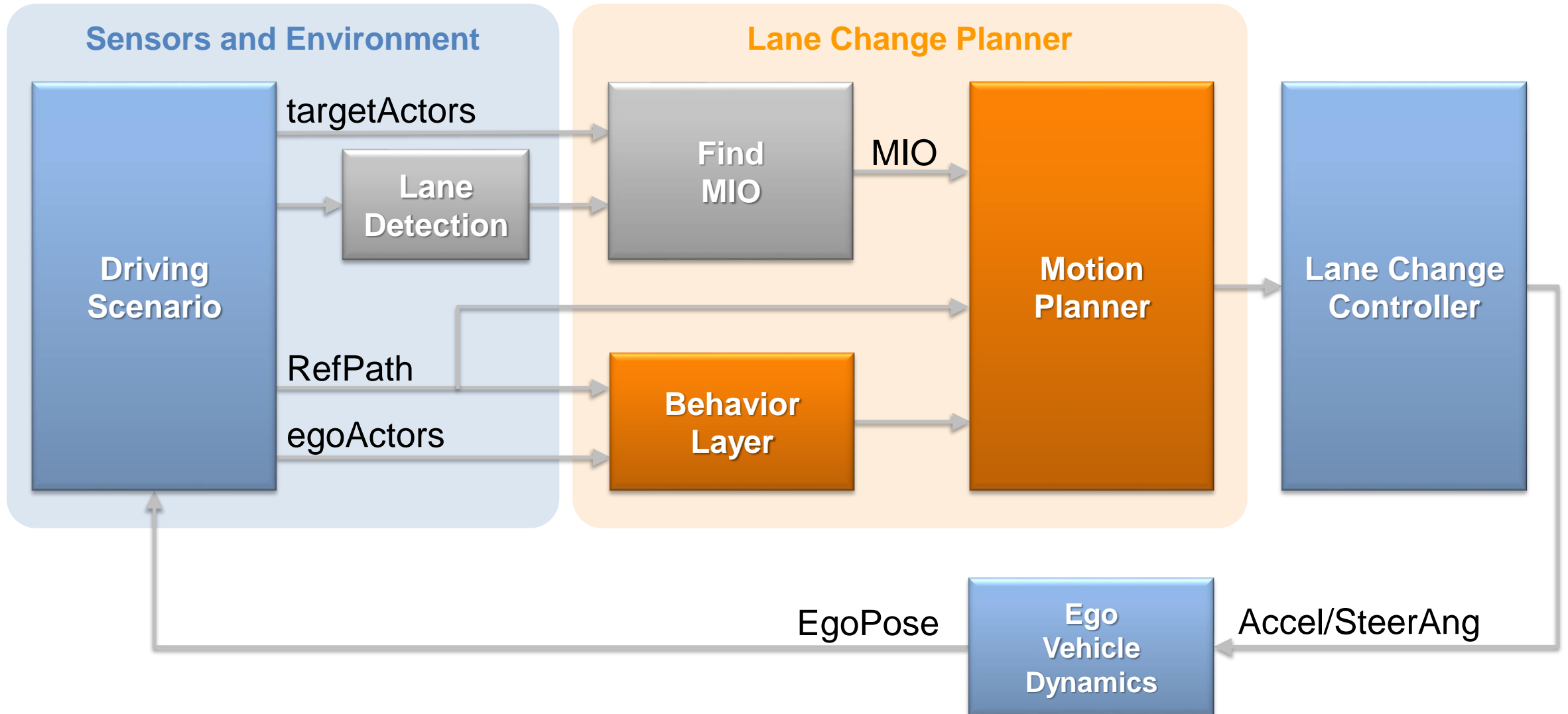
Test with real-world scenario

- Create scenario from HD map
- Update setup script and model
- Run simulation with new scenario

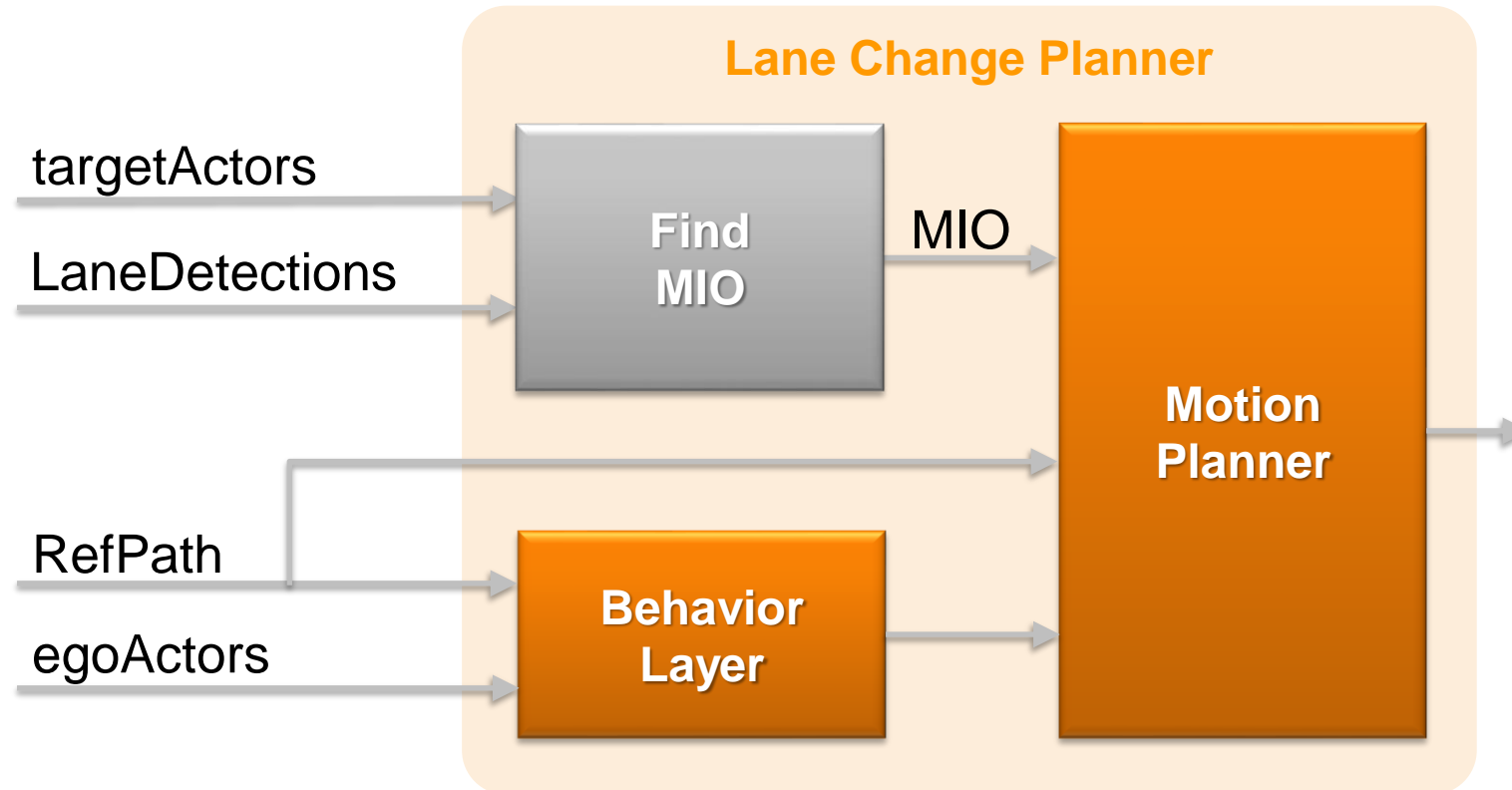
Test Bench Model for Highway Lane Change



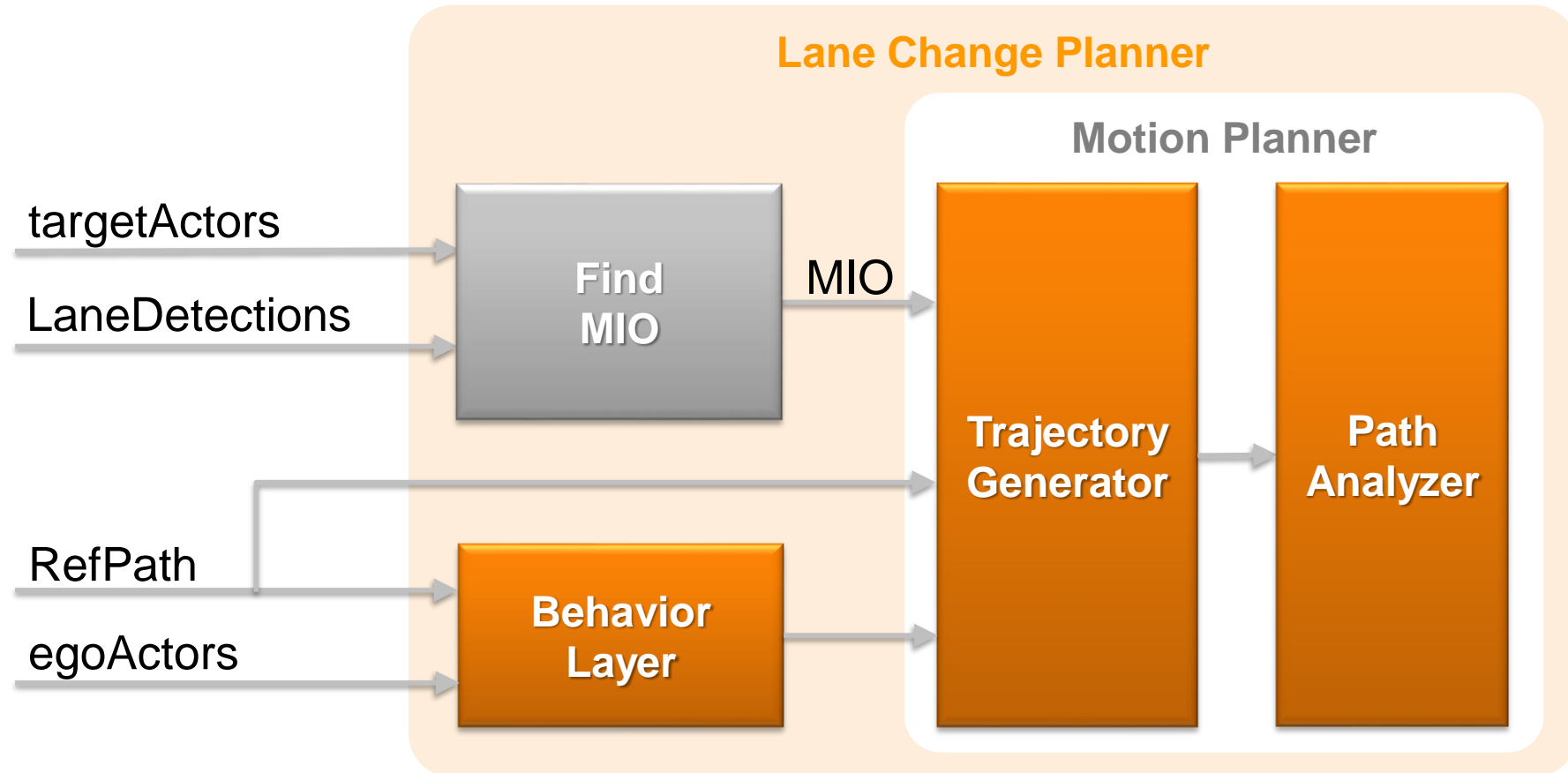
Architecture of Highway Lane Change



Lane Change Planner

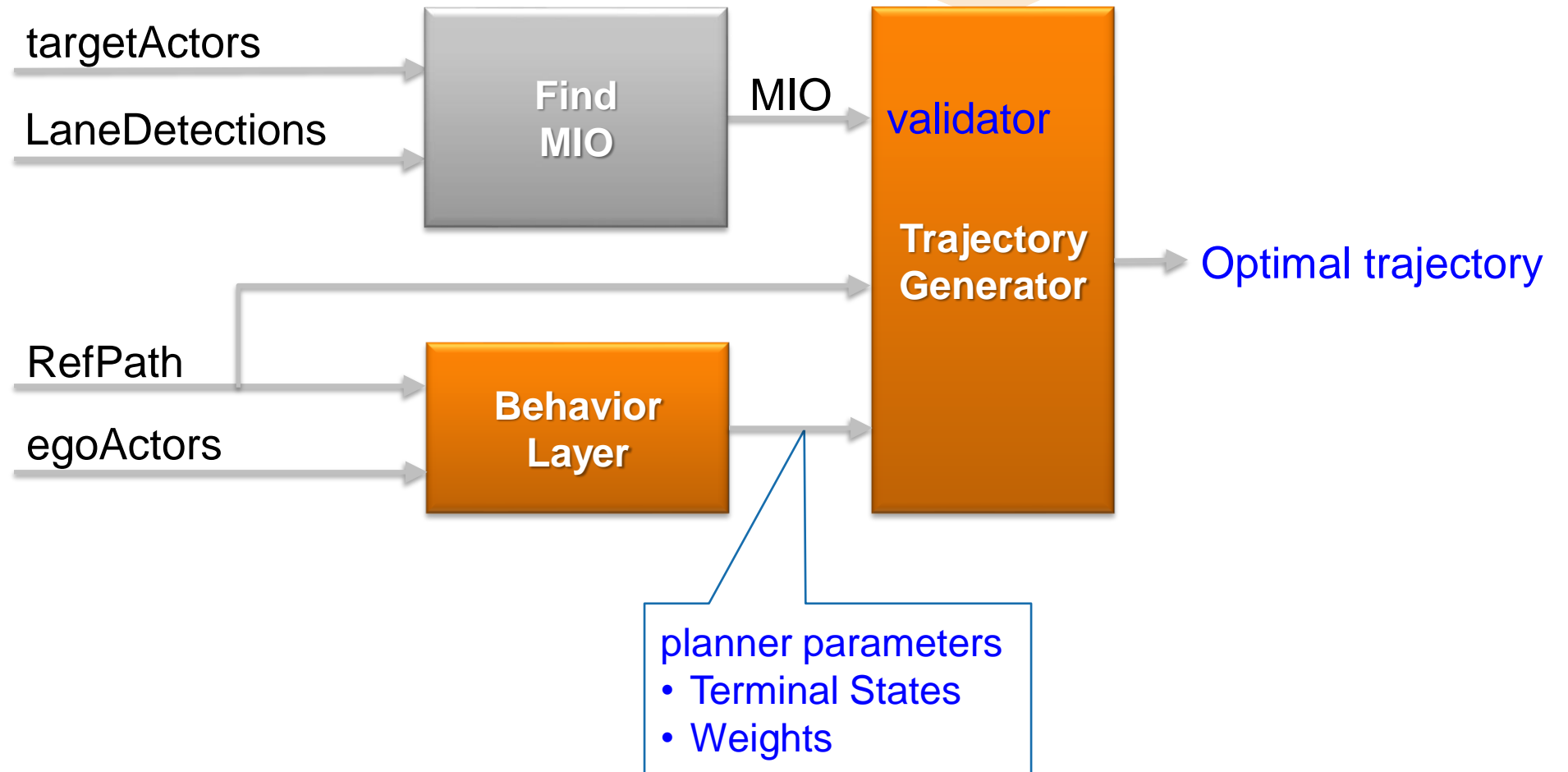


Lane Change Planner

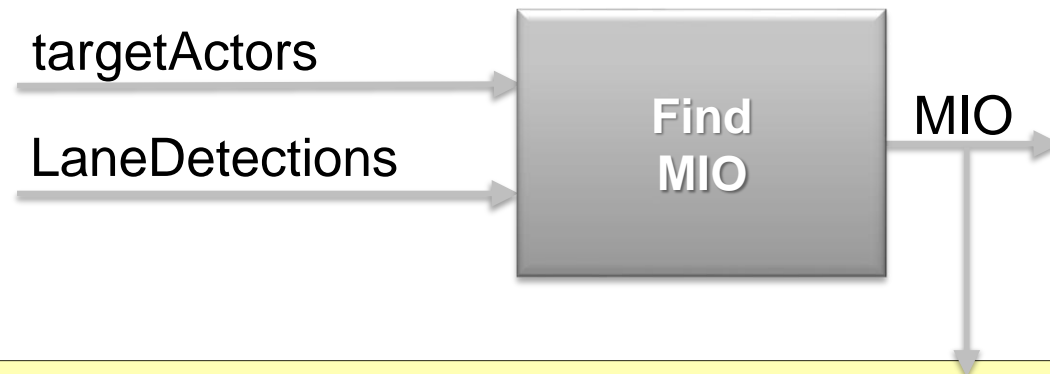


Lane Change Planner

```
planner = trajectoryOptimalFrenet(refPath, validator)
```

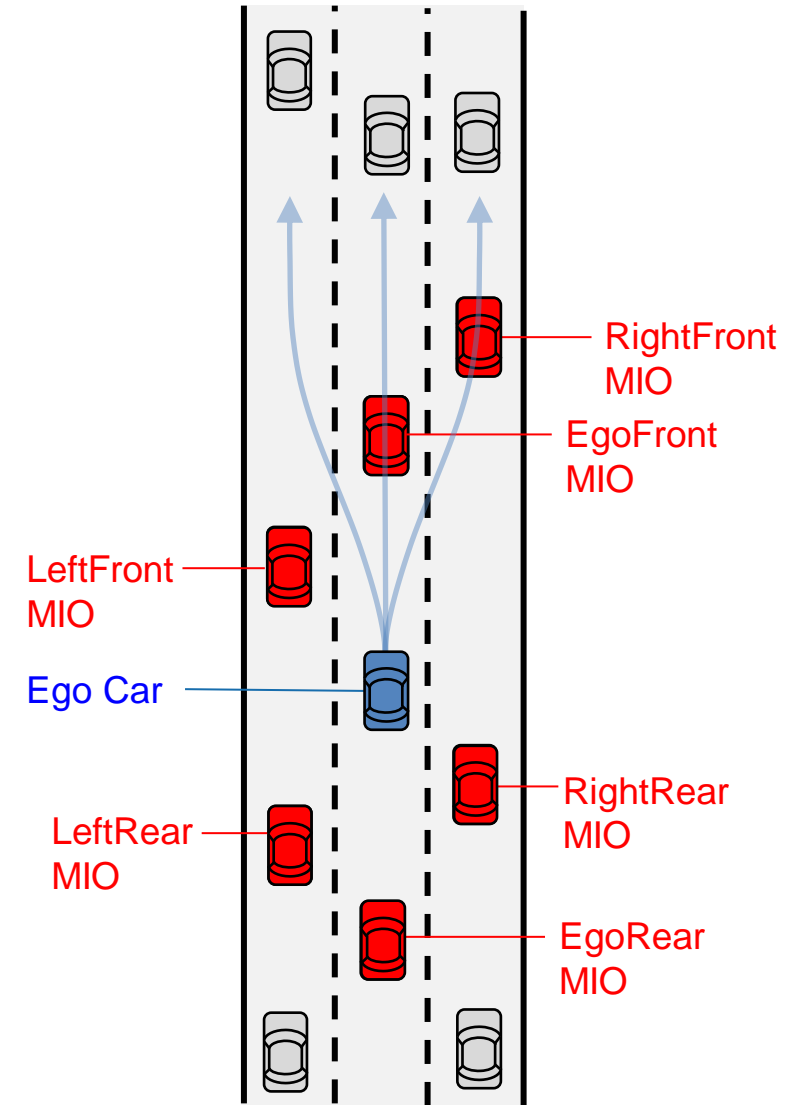


Find Most Important Objects (MIO)



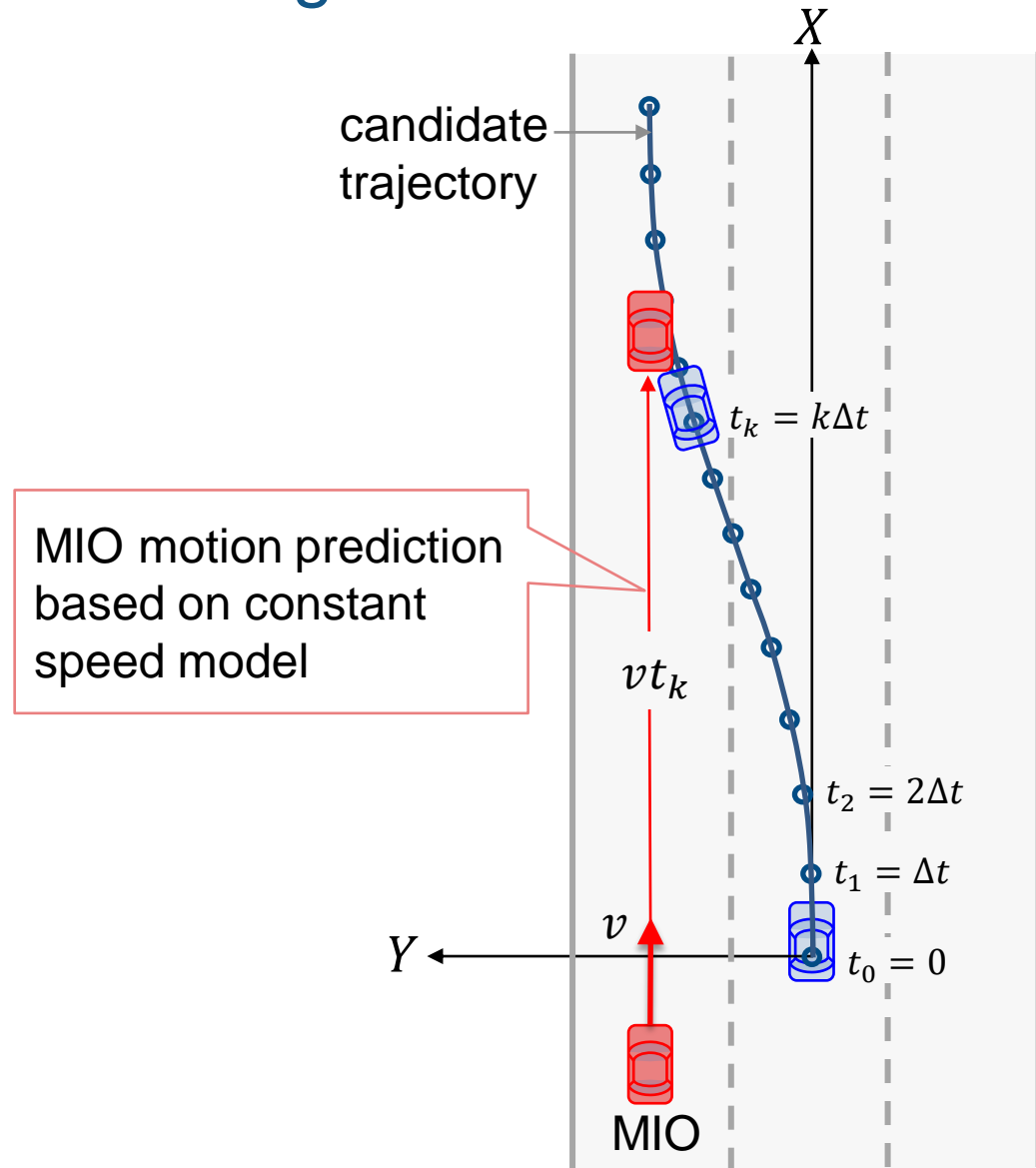
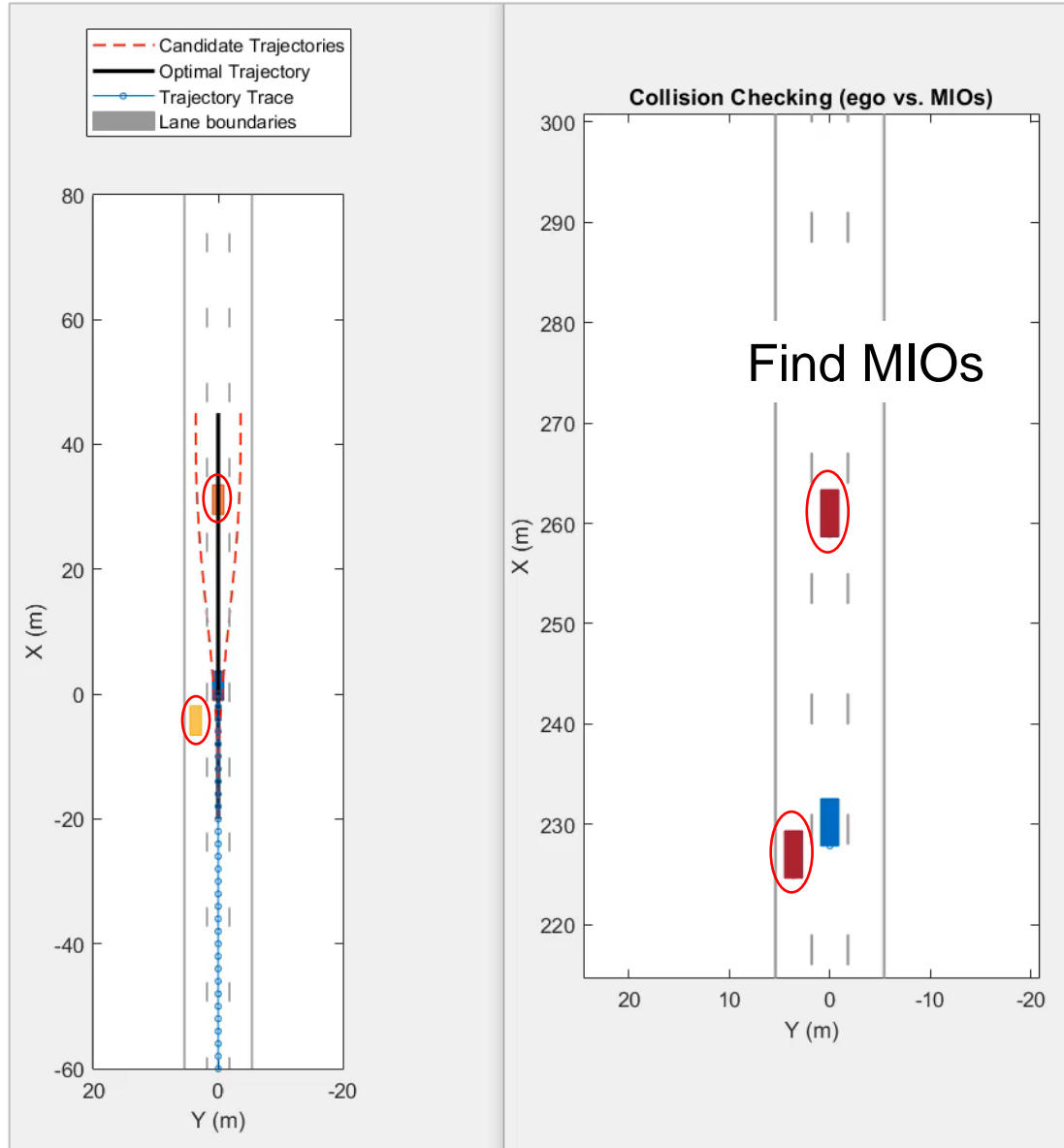
```
planner = trajectoryOptimalFrenet(refPath, validator)
```

- Find MIOs in ego and neighbor lanes
- MIOs are provided for the custom state validator for collision checking.



Max. 6 MIOs

Custom State Validator for Collision checking



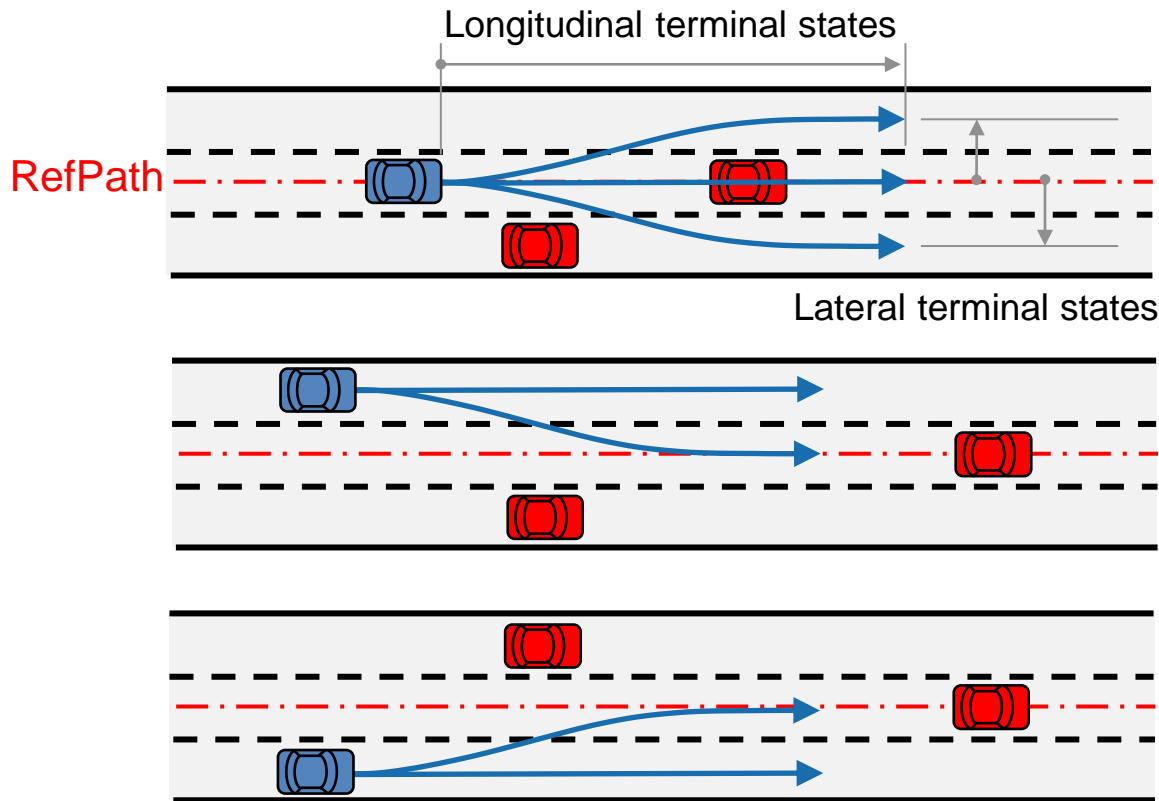
Behavior Layer

RefPath

egoActors



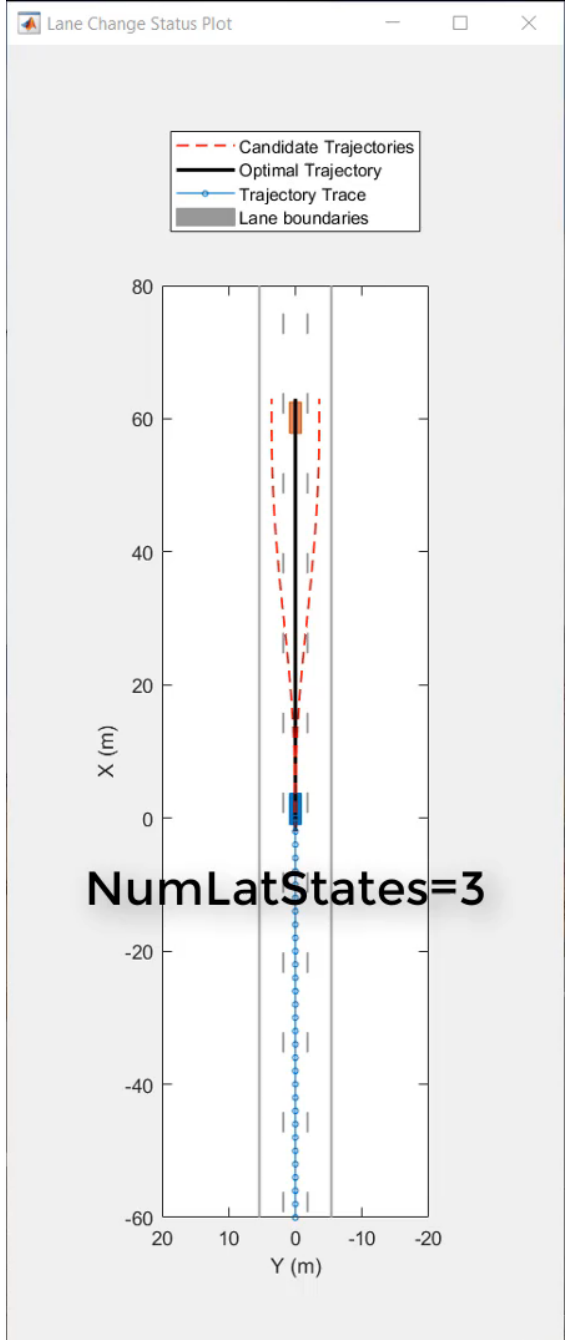
planner parameters
 • Terminal States
 • Weights



NumLatStates = 3

NumLatStates = 2
(No Left Lane)

NumLatStates = 2
(No Right Lane)



Motion Planner ▷ Trajectory Generator

```
planner = trajectoryOptimalFrenet(refPath, validator)
```

MIO

RefPath

Planner Parameters

- Terminal States
- Weights

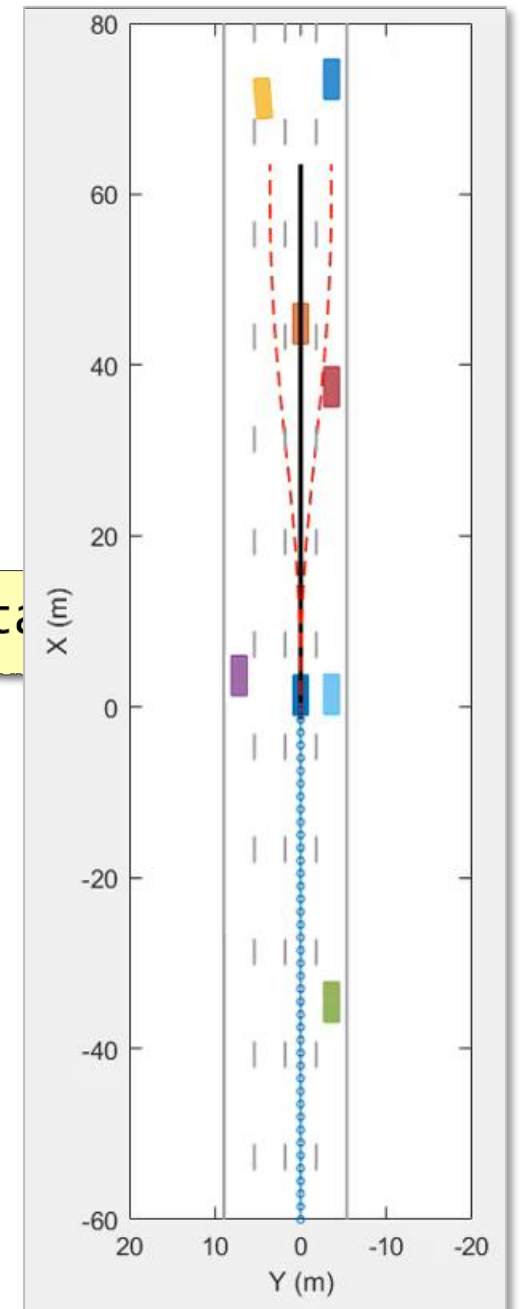
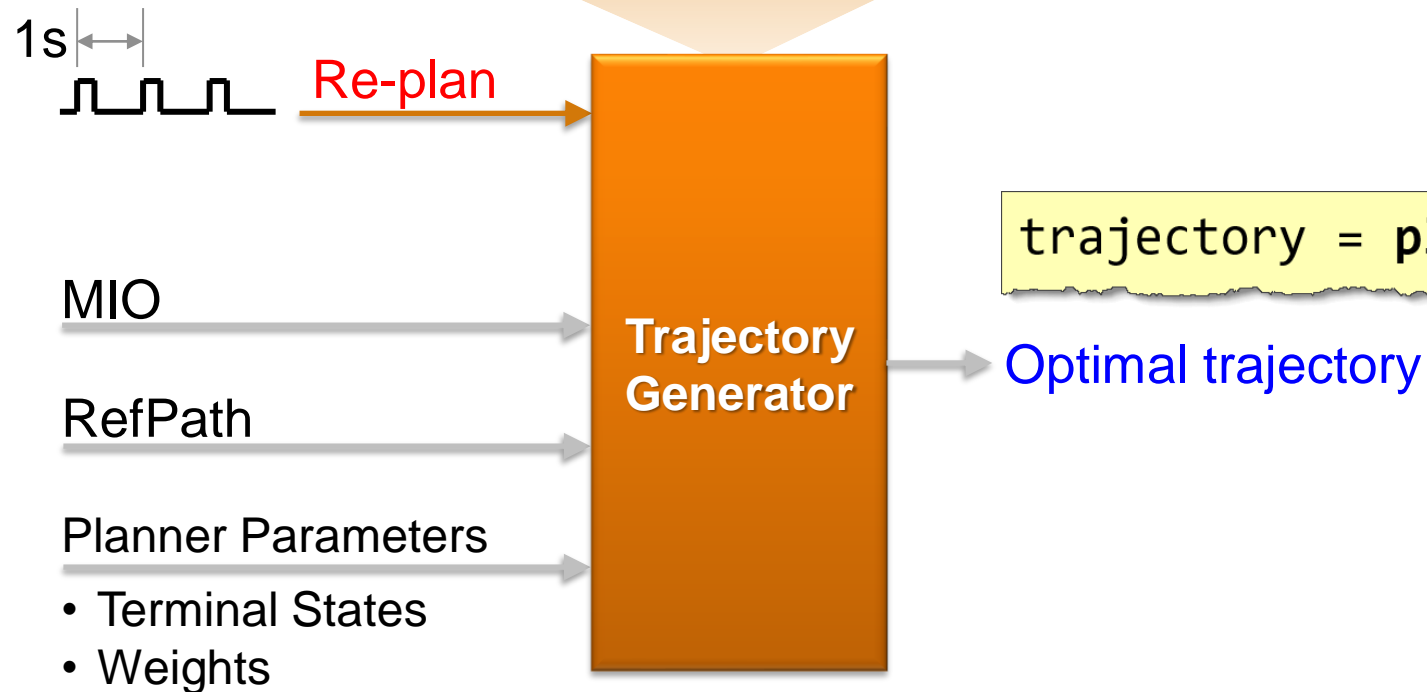
Trajectory
Generator

```
trajectory = plan(planner, startFrenetState)
```

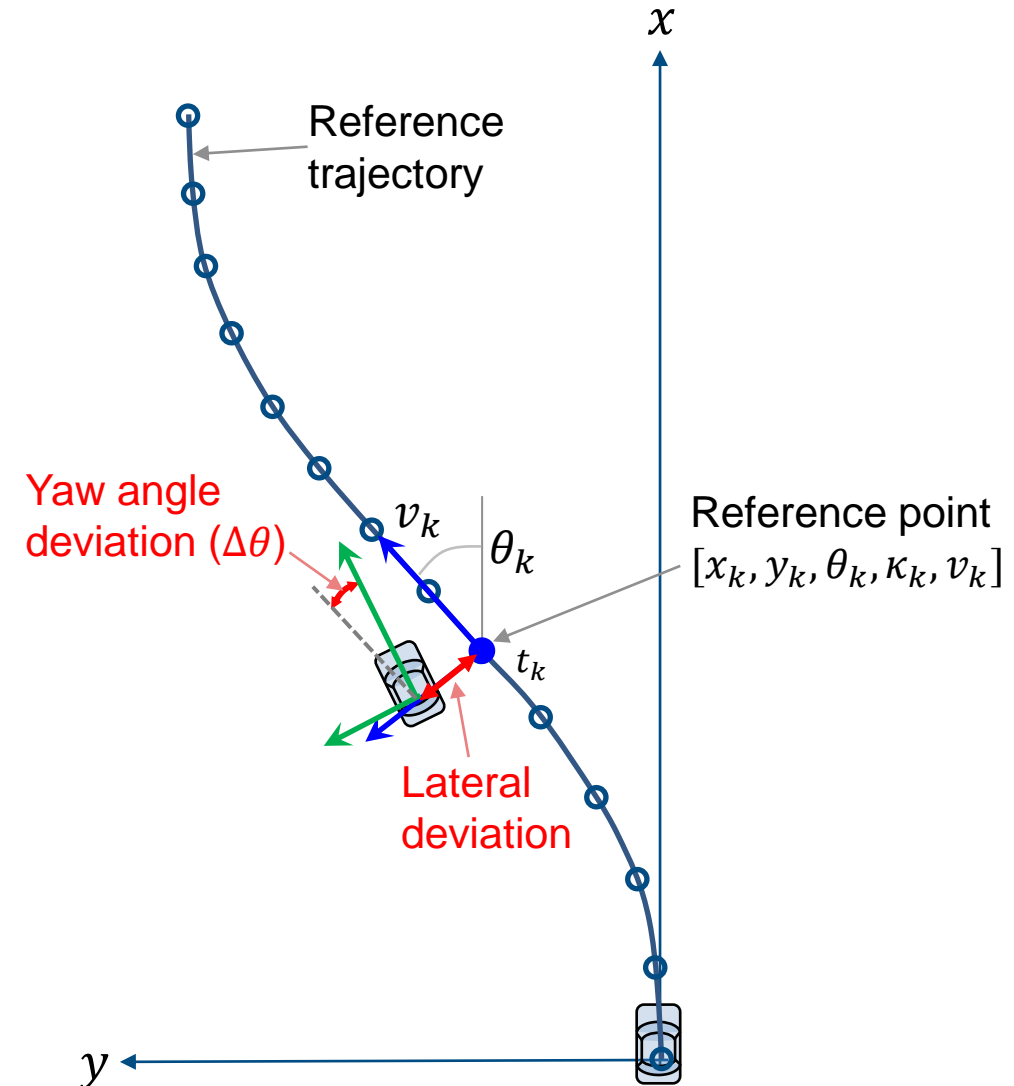
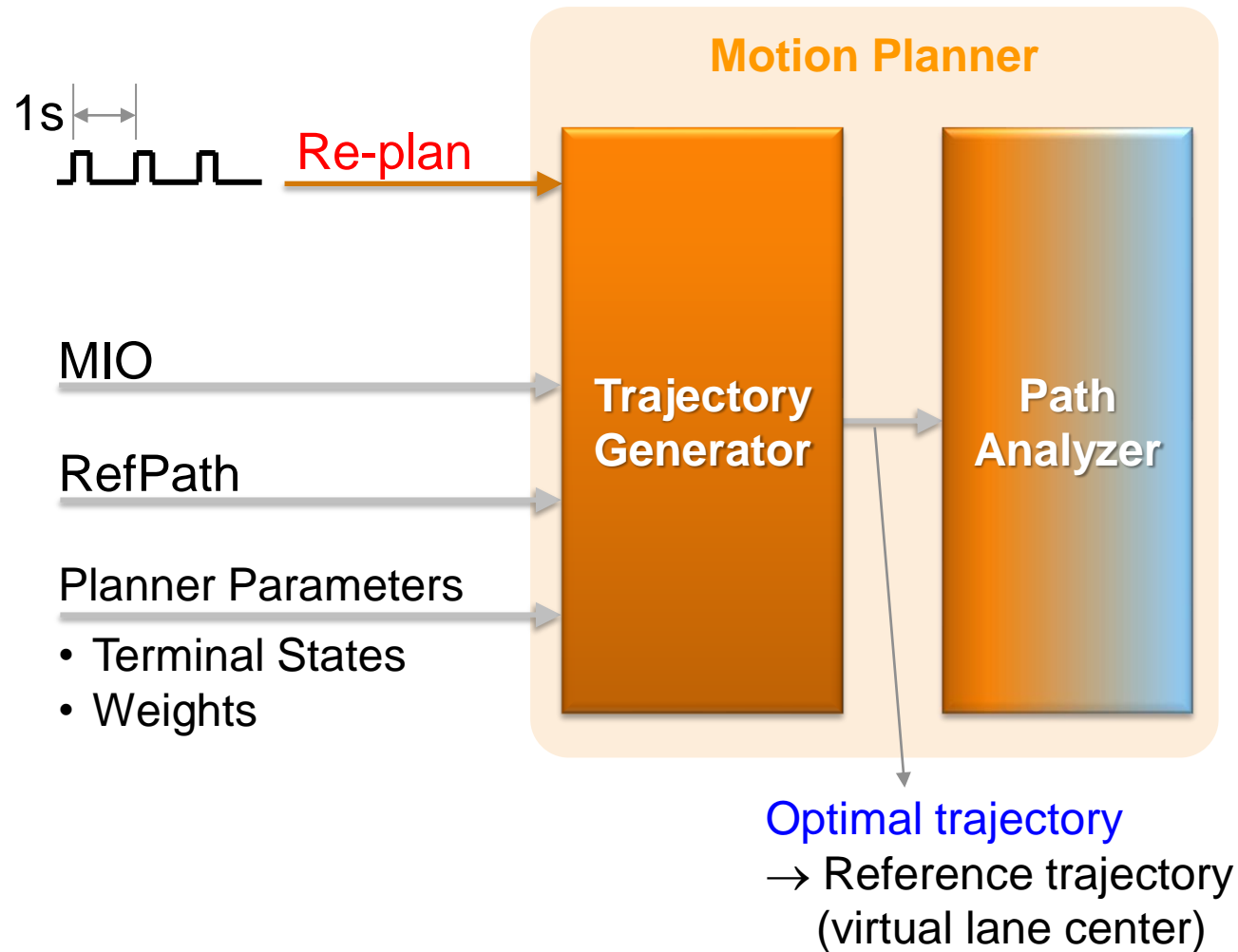
Optimal trajectory

Motion Planner ▷ Periodic Re-planning

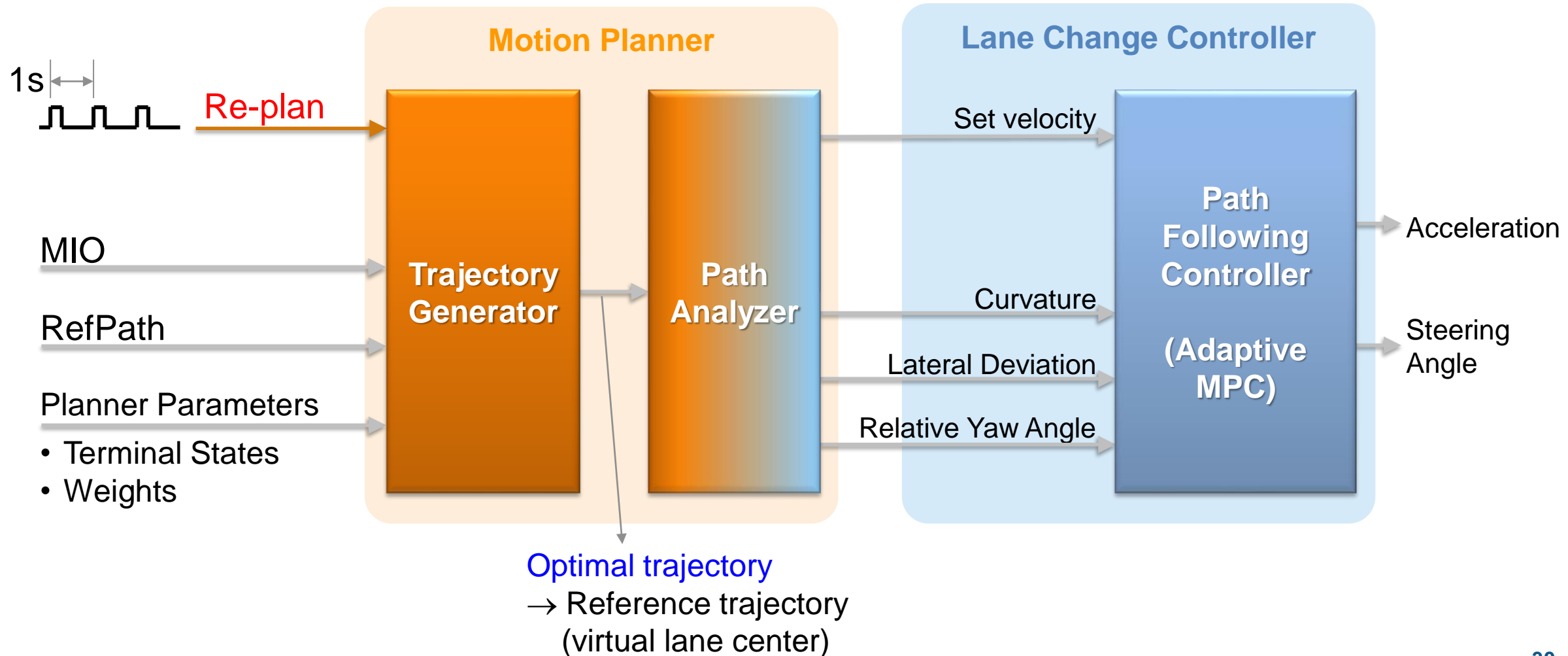
```
planner = trajectoryOptimalFrenet(refPath, validator)
```



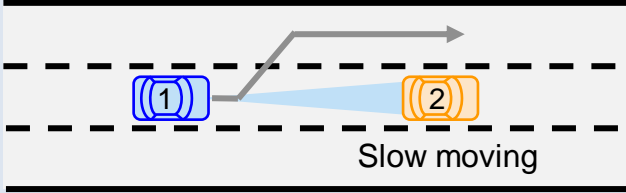
Motion Planner ▷ Path Analyzer



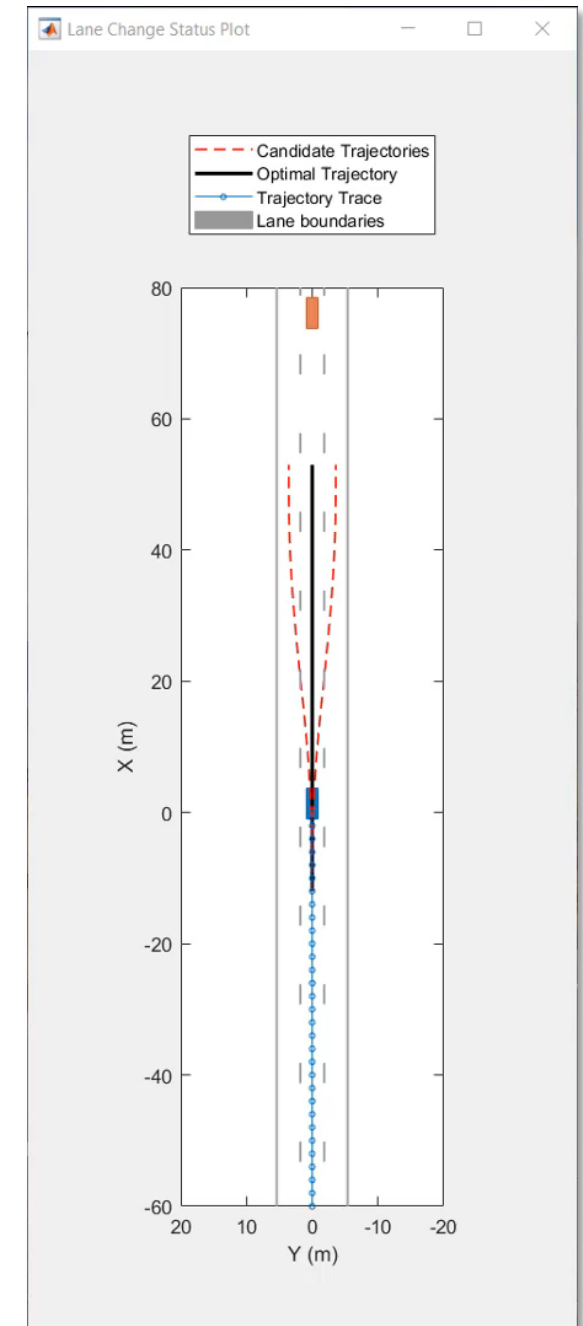
Motion Planner and Lane Change Controller



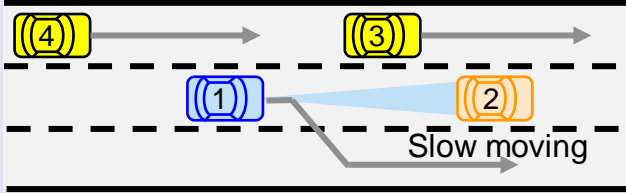
Simulate Highway Lane Change with Test Scenarios

Test Name	scenario_LC_01_SlowMoving
Test Description	Passing slow moving lead car 
(1) Host Car	initial velocity = 20m/s HWT = 6.5sec HW = 130m v_set = 20m/s
(2) Lead Car	constant velocity = 10m/s
Other Cars	None

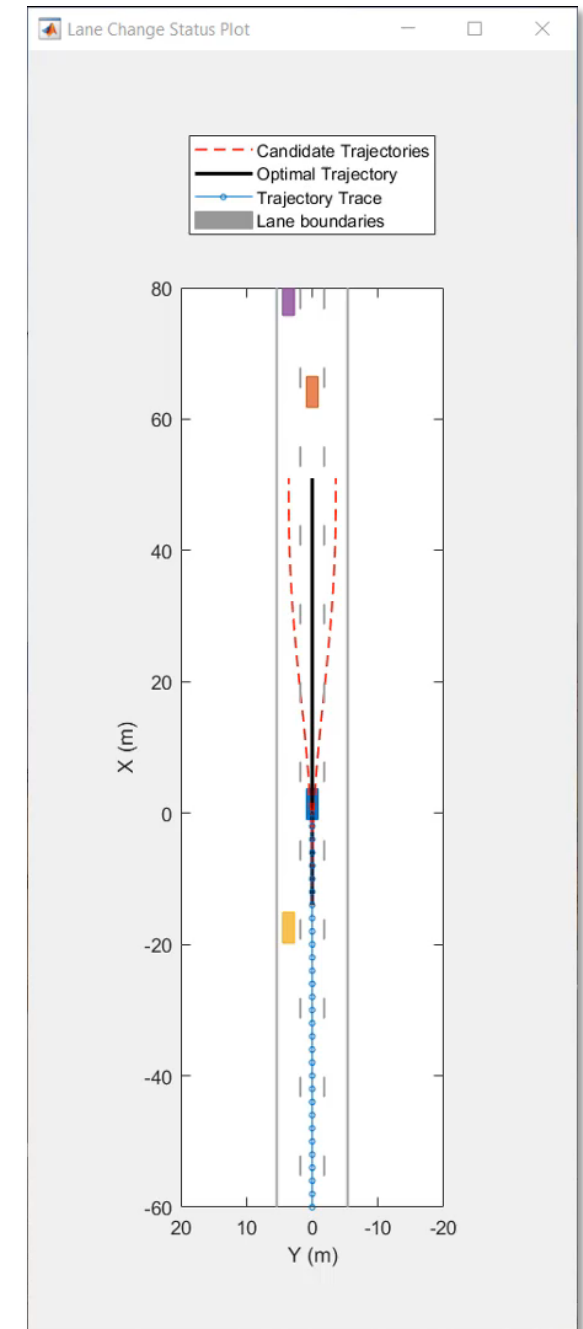
HWT : Headway time
 HW : Headway
 v_set : set velocity for ego car



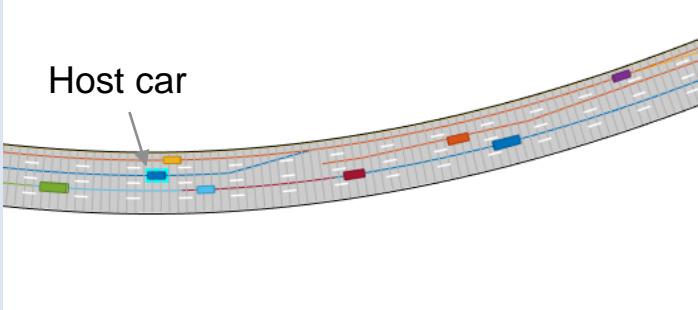
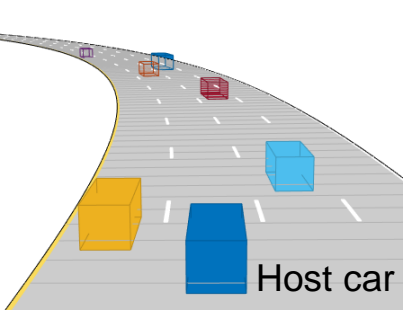
Simulate Highway Lane Change with Test Scenarios

Test Name	scenario_LC_07_RightLaneChange
Test Description	Passing slow moving lead car to right lane 
(1) Host Car	initial velocity = 20m/s HWT = 6sec HW = 120m v_set = 20m/s
(2) Lead Car	constant velocity = 10m/s
Other Cars	Constant velocity = 25m/s (3 rd car in left lane) Constant velocity = 24m/s (4 th car in left lane)

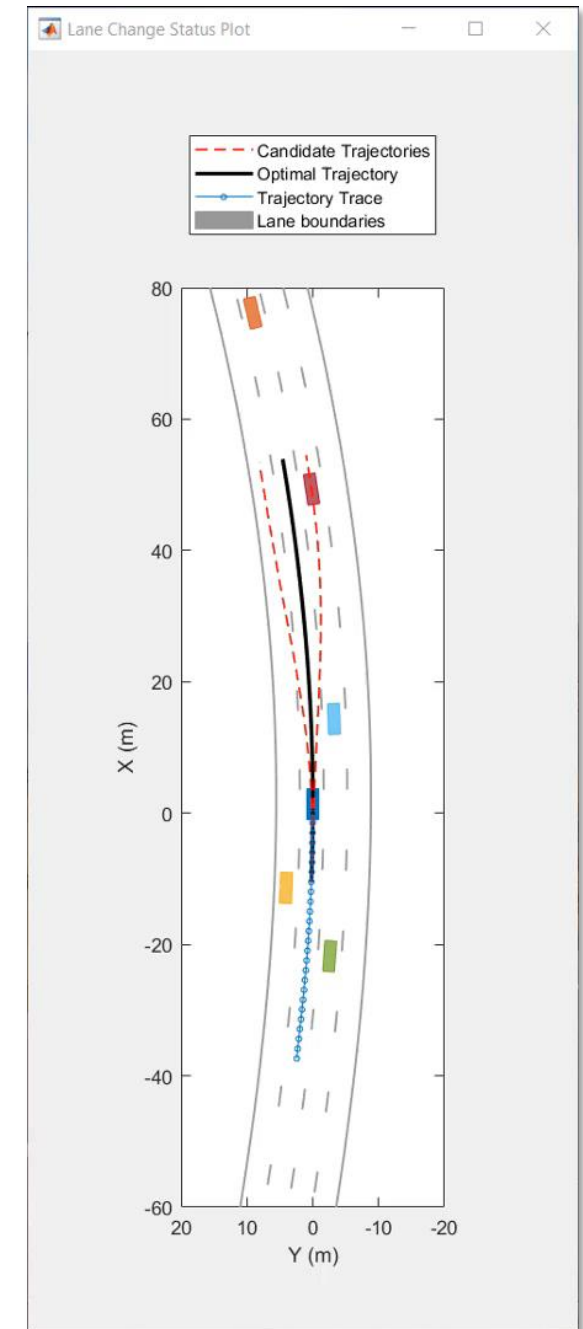
HWT : Headway time
 HW : Headway
 v_set : set velocity for ego car



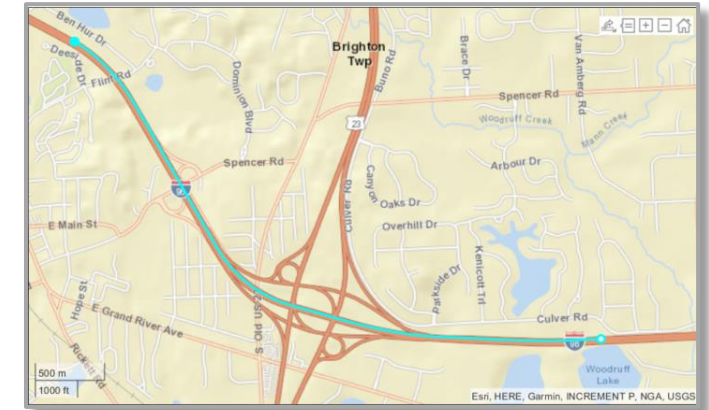
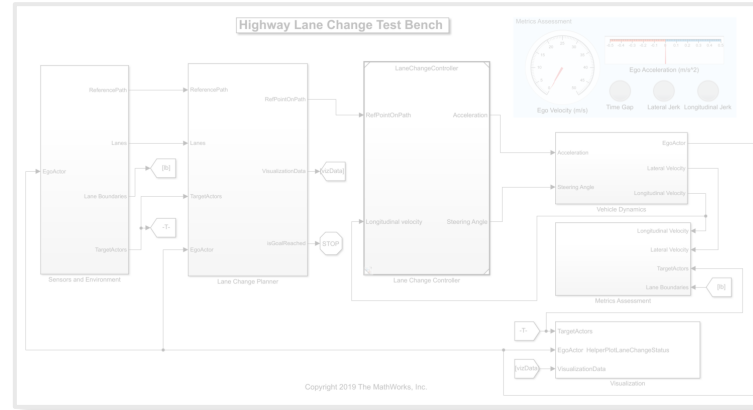
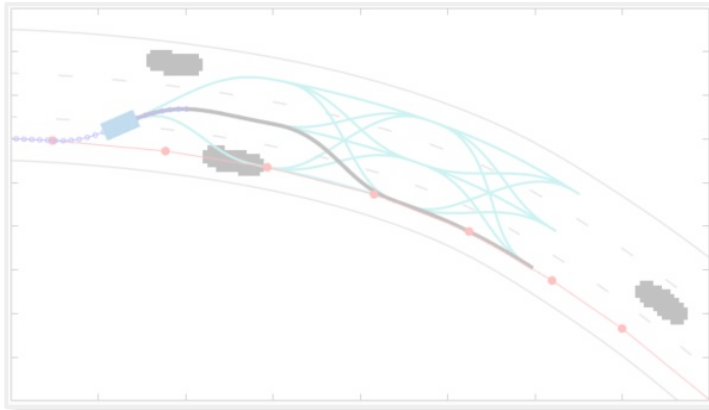
Simulate Highway Lane Change with Test Scenarios

Test Name	scenario_LC_10_SingleLaneChange_Curved
Test Description	Passing slow moving lead car to left lane in curved road <div style="display: flex; justify-content: space-around; margin-top: 10px;">   </div>
(1) Host Car	initial velocity = 15m/s $v_set = 15\text{m/s}$
(2) Lead Car	Slow moving
Other Cars	Dense traffic

HWT : Headway time
 HW : Headway
 v_set : set velocity for ego car



Highway Lane Change



Learn motion planner

- Optimal trajectory generation in Frenet coordinate
- Planner parameters
- Simulate trajectory planning with occupancy map

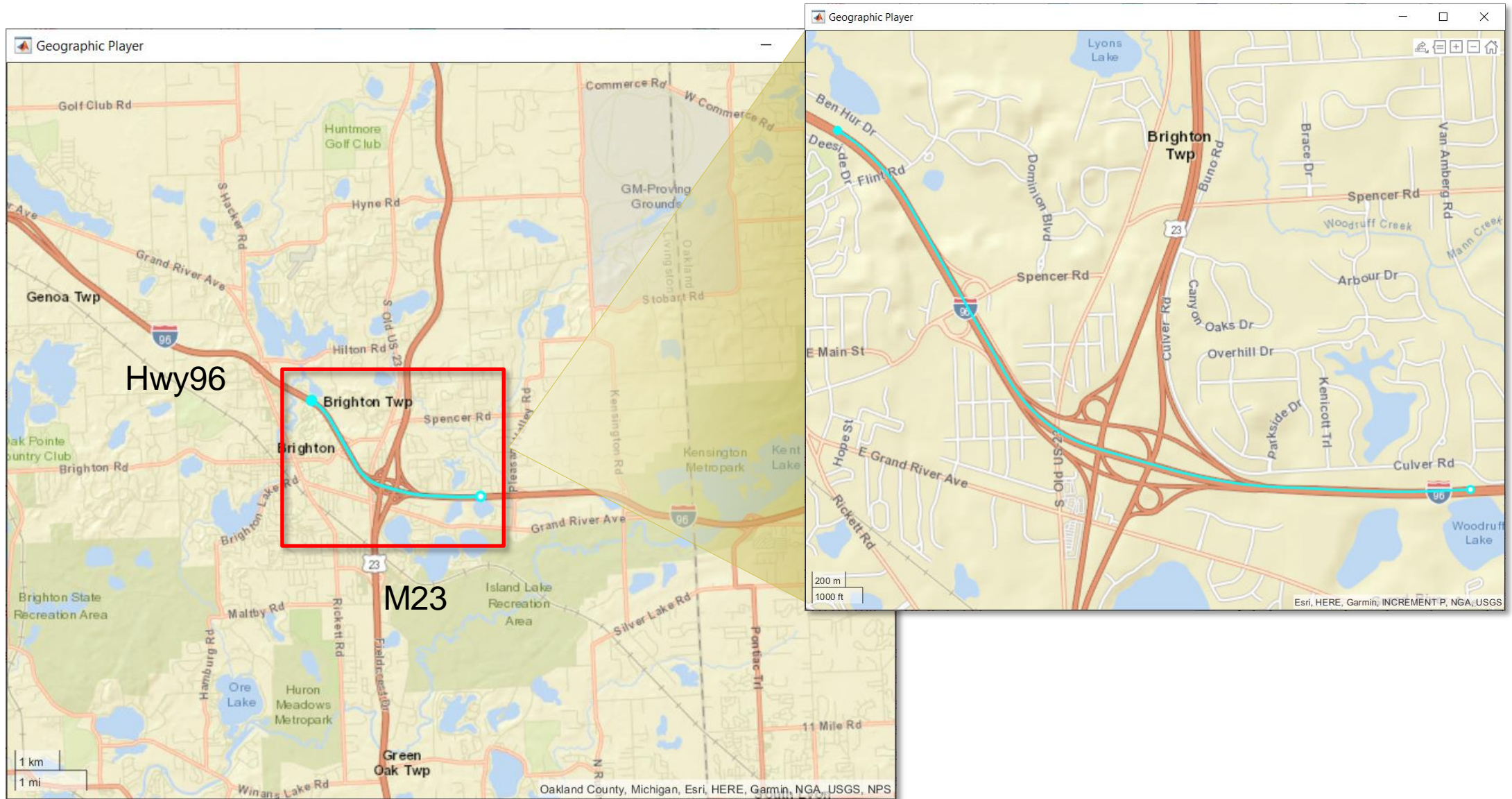
Integrate motion planner and controller

- Learn through reference example
- Architecture of highway lane change
- Simulate closed-loop controller with test scenarios

Test with real-world scenario

- Create scenario from HD map
- Update setup script and model
- Run simulation with new scenario

Create highway road network from HD map



Import HERE HD Live Map into Driving Scenario

DESIGNER

New Open Save Import Add Road Add Actor Add Camera Add Radar

FILE

Roads Acto

Road:

Name:

Width (m):

Bank Angle (deg):

Lanes

Road Centers

OpenDRIVE Road Network
Import roads from .xml or .xodr OpenDRIVE files

HERE HD Live Map
Import roads generated from HERE HD Live Map data (credentials required)

HERE HD Live Map Import

Specify Geographic Coordinates

From Workspace Input Coordinates

Latitude Latitude Longitude Longitude

Select Region

Specify a region around the roads of interest.

1 km
0.5 mi

Cancel Back

HERE HD Live Map Import

Specify Geographic Coordinates

From Workspace Input Coordinates

Latitude Latitude Longitude Longitude

Select Roads

Select a road by clicking on it. Select multiple roads with controls in the toolbar.

500 m
2000 ft

Select All Deselect All

Cancel Back Import

Add actors and export driving scenario with MATLAB Function

The screenshot shows the Driving Scenario Designer interface. The 'Export MATLAB Function' button is highlighted with a red box. The button text is: **Export MATLAB Function**
Generate MATLAB function for your driving scenario and sensors.

The MATLAB code generated by the software is as follows:

```
function [scenario, egoVehicle] = createDrivingScenario()
% createDrivingScenario Returns the drivingScenario defined in
% Generated by MATLAB(R) 9.8 (R2020a) and Automated Driving Tool
% Generated on: 24-Mar-2020 17:27:39
% Construct a drivingScenario object.
scenario = drivingScenario('StopTime', 19, ...
    'SampleTime', 0.1);
% Add all road segments
roadCenters = [57.03213 -1223.454 0;
    52.57648 -1138.823 0;
    40.3209 -862.7384 0;
    35.85877 -764.1326 0;
    35.85681 -746.0532 0;
    35.85499 -728.8004 0;
    30.29402 -607.1907 0;
```

Setup driving scenario and workspace variables

```
function helperSLHighwayLaneChangeSetup(varargin)

%% Inputs
% Scenario function name
defaultScenarioFcnName = "scenario_LC_06_DoubleLaneChange";
validScenarioFcnNames = [...
    "scenario_LC_01_SlowMoving"
    "scenario_LC_02_SlowMovingWithPassingCar"
    "scenario_LC_03_DisabledCar"
    "scenario_LC_04_CutInWithBrake"
    "scenario_LC_05_SingleLaneChange"
    "scenario_LC_06_DoubleLaneChange"
    "scenario_LC_07_RightLaneChange"
    "scenario_LC_08_SlowmovingCar_Curved"
    "scenario_LC_09_CutInWithBrake_Curved"
    "scenario_LC_10_SingleLaneChange_Curved"
    "scenario_LC_11_Hwy96_M23_WithMergingCar"
    "scenario_LC_12_Hwy96_M23_WithCutInCar"];
```

Add new driving
scenario

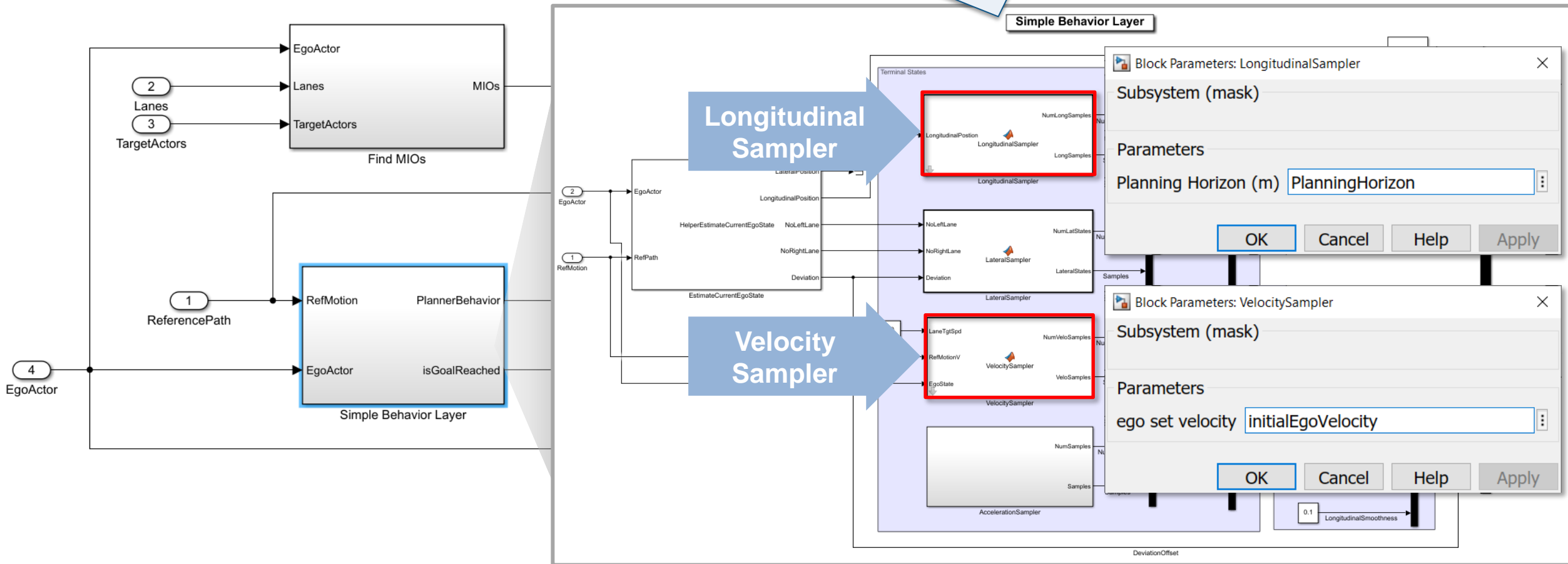
Command Window

```
>> helperSLHighwayLaneChangeSetup("scenario_LC_11_Hwy96_M23_WithMergingCar")
fx>> |
```

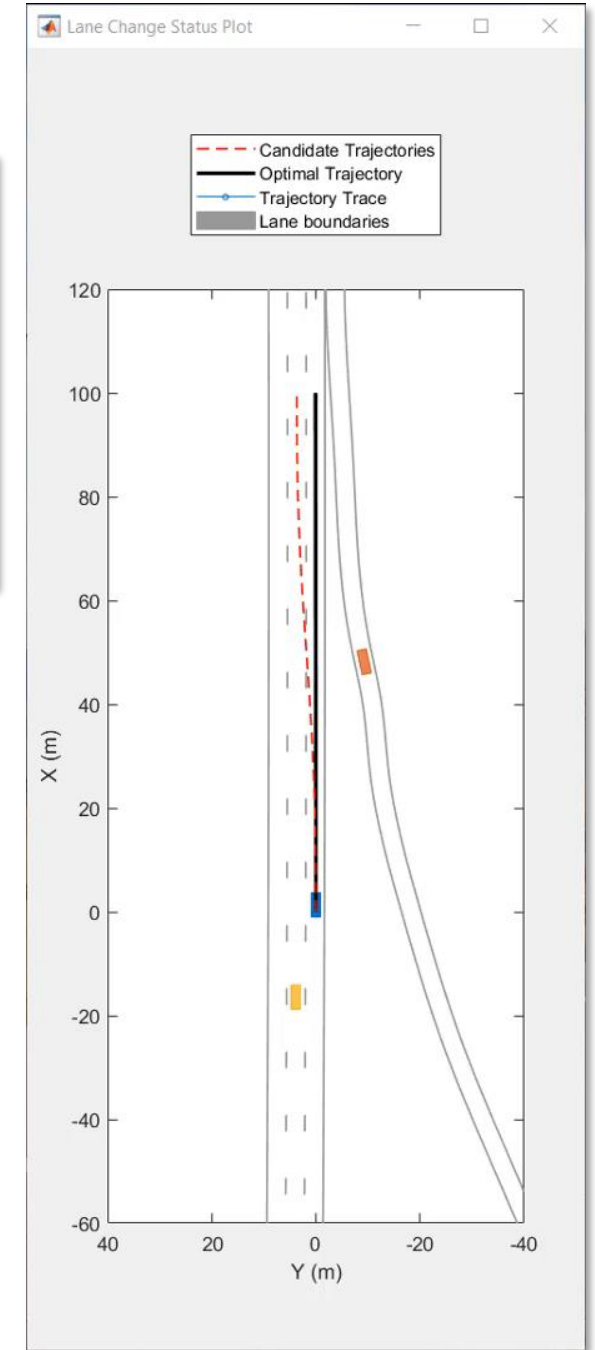
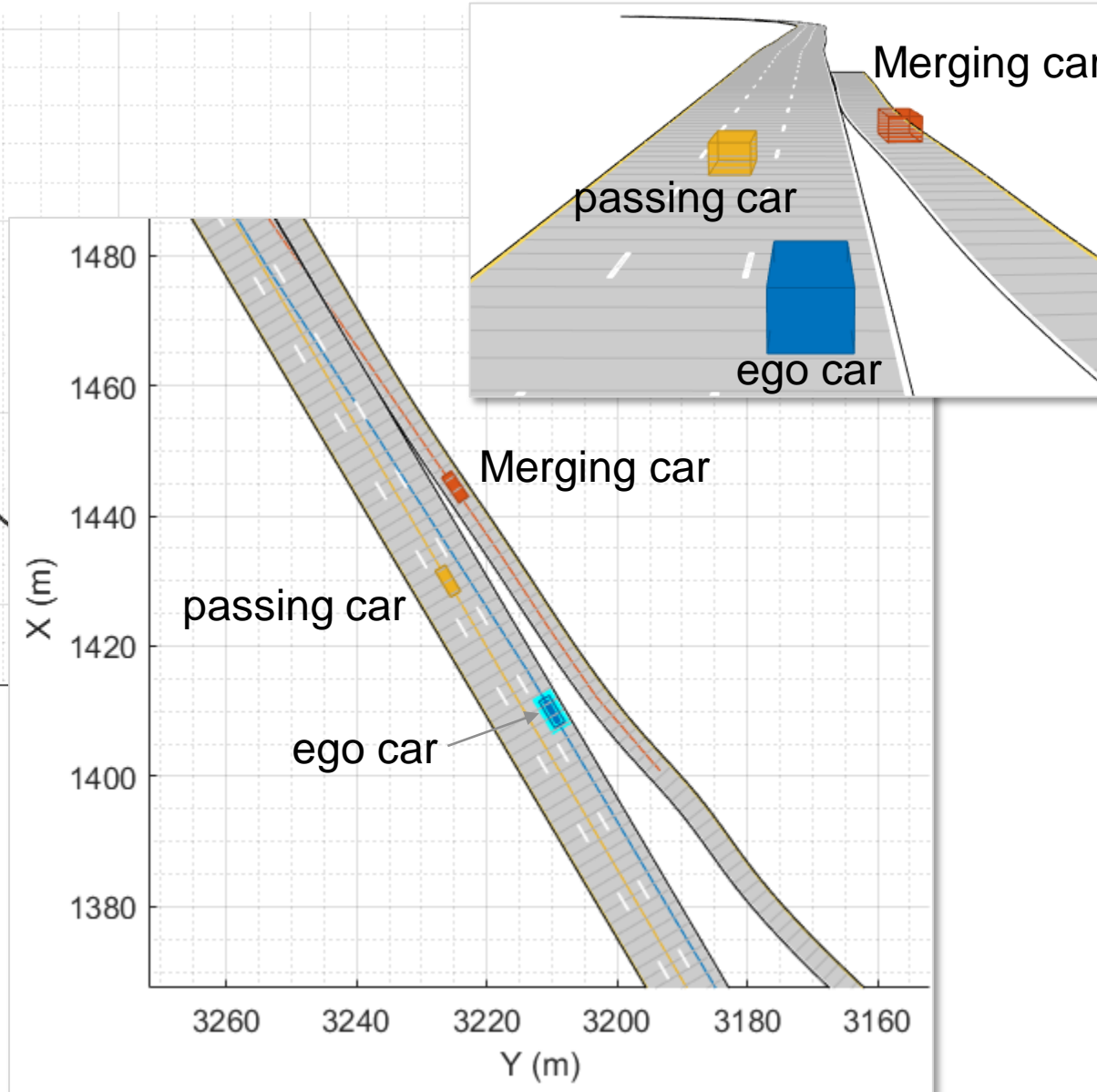
Update Lane Change Planner ▷ Simple Behavior Layer

Lane Change Planner

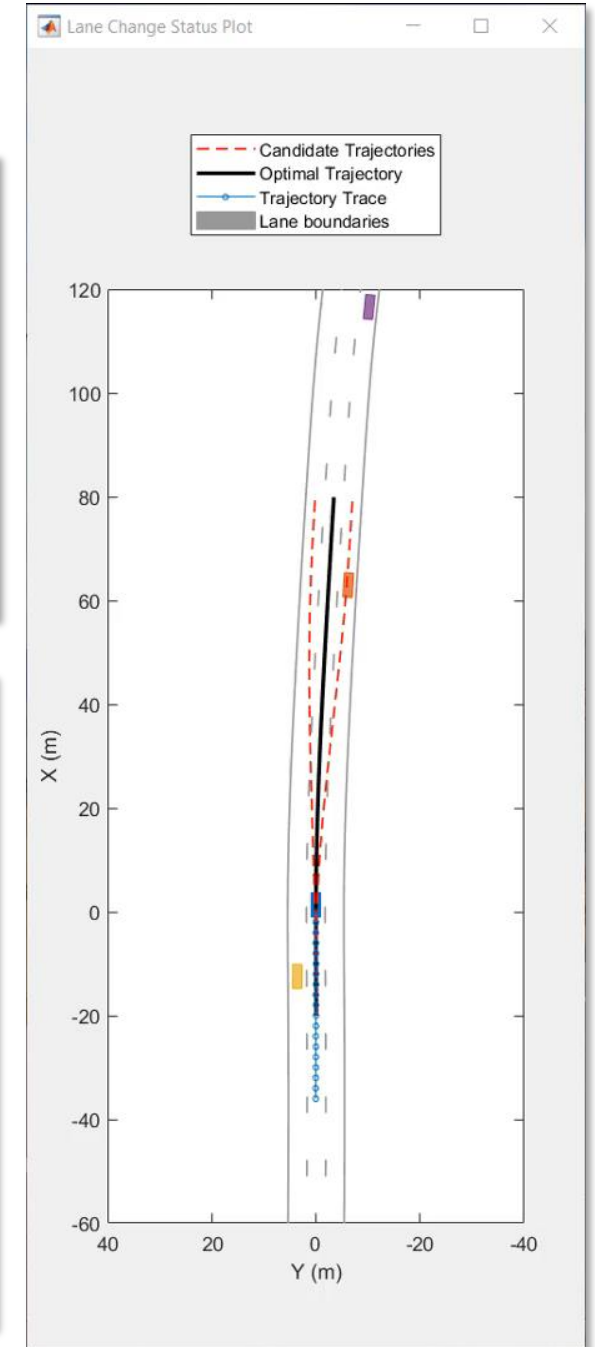
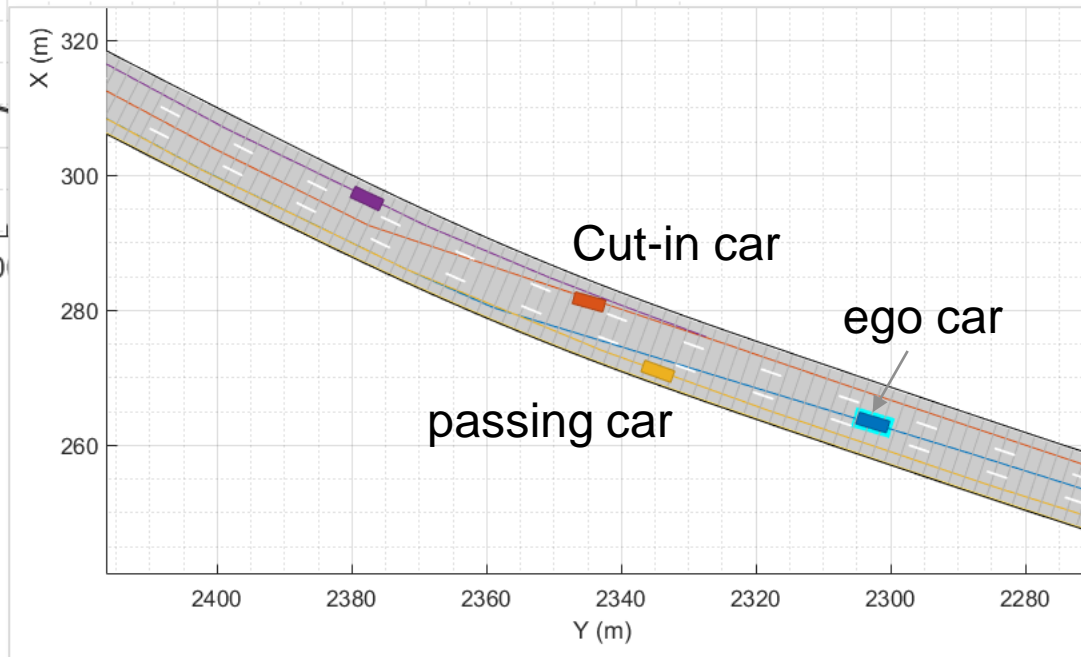
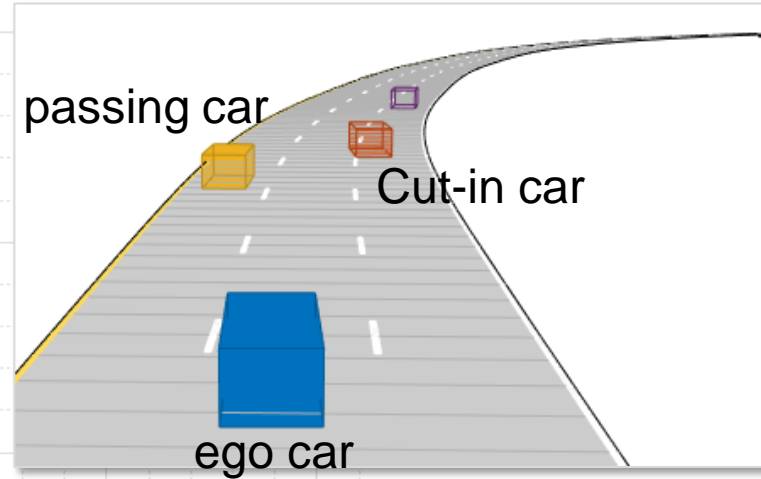
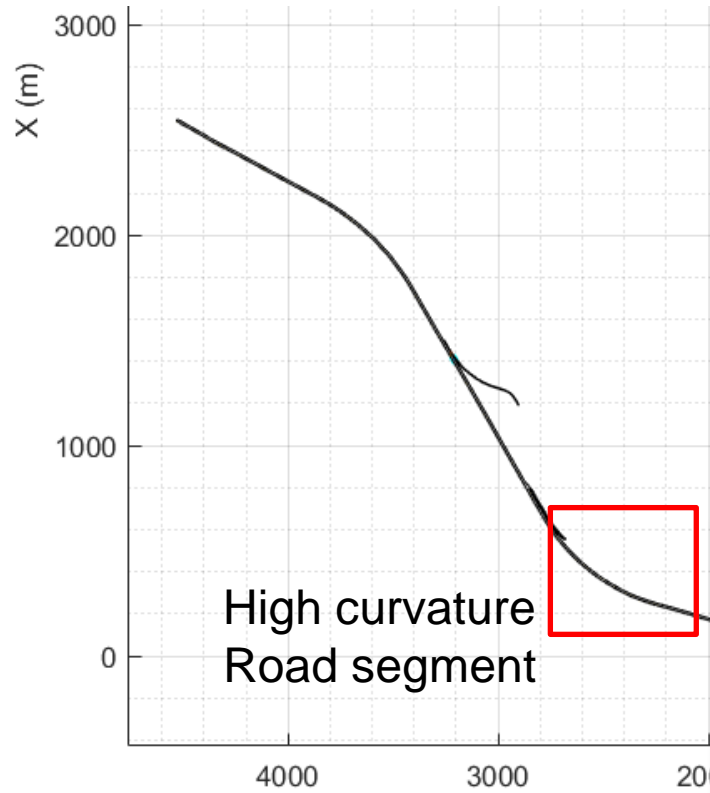
Update longitudinal & velocity sampler to read input parameter



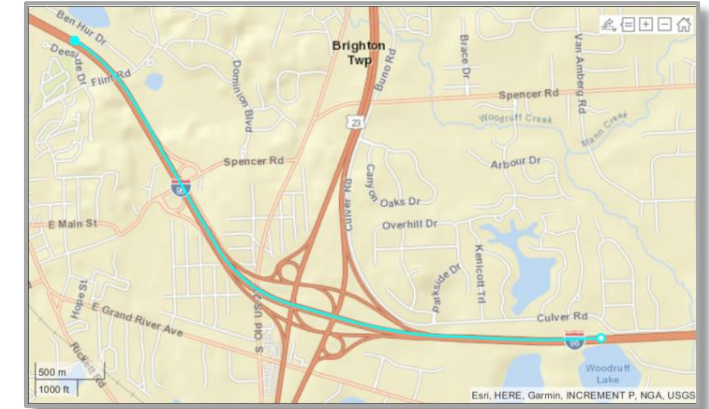
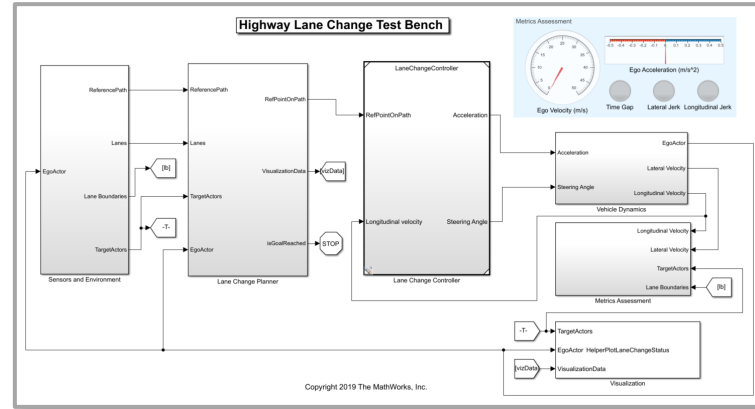
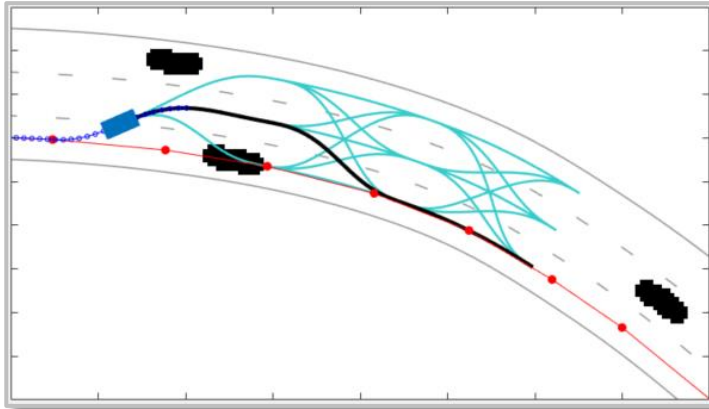
scenario_LC_11_Hwy96_M23_WithMergingCar



scenario_LC_12_Hwy96_M23_WithCutInCar



Recap: Highway Lane Change



Learn motion planner

- Optimal trajectory generation in Frenet coordinate
- Planner parameters
- Simulate trajectory planning with occupancy map

Integrate motion planner and controller

- Learn through reference example
- Architecture of highway lane change
- Simulate closed-loop controller with test scenarios

Test with real-world scenario

- Create scenario from HD map
- Update setup script and model
- Run simulation with new scenario

Presenter contact info and poll questions

Please contact me at spark@mathworks.com with questions

- Poll question : I found this technique the most interesting
 - a. Motion planner for lane change
 - b. MPC path following controller
 - c. Driving scenario creation
 - d. Import HD map into driving scenario
- If you would like to an individual follow-up, please let us know in the WebEx poll area.